

Transformations of Correlated Electronic States by Electric or Optical Impacts.

International research school and workshop IMPACT – 2024

August 27, 2024

Cargèse, France

Photoinduced Symmetry Breaking, Off-Diagonal Conductivity and Magnetism

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Supported by MEXT Q-LEAP Grant Number JPMXS0118067426,

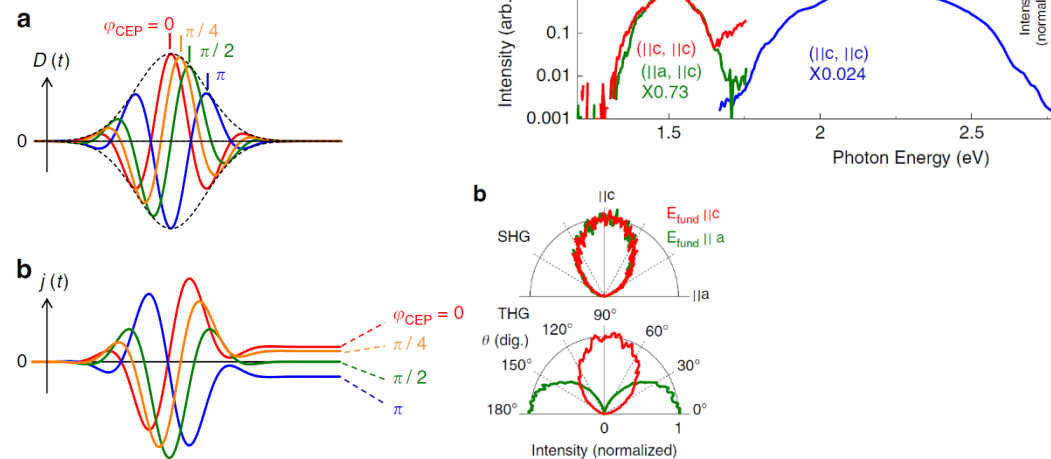
JST CREST Grant Number JPMJCR1901, Japan

From photoinduced phase transitions To manipulation of states **directly by light**

- **Symmetry** of electronic states modified by light
- Using linearly polarized (LP), circularly polarized (CP), or bicircular (BC) light
- In this talk, states **during** the photoirradiation are the main topic.
- Before the main topic
- One example where the symmetry is modified just after irradiation
- SHG in an organic SC caused by **transient** breaking of inversion symmetry through CEP controlled linearly polarized light

Y. Kawakami et al., Nat. Commun. 11, 4138 (2020).

-- This SHG is transient.



Laser light can break time-reversal/ space-inversion/ mirror symmetry by choosing CP, BC, or LP light.

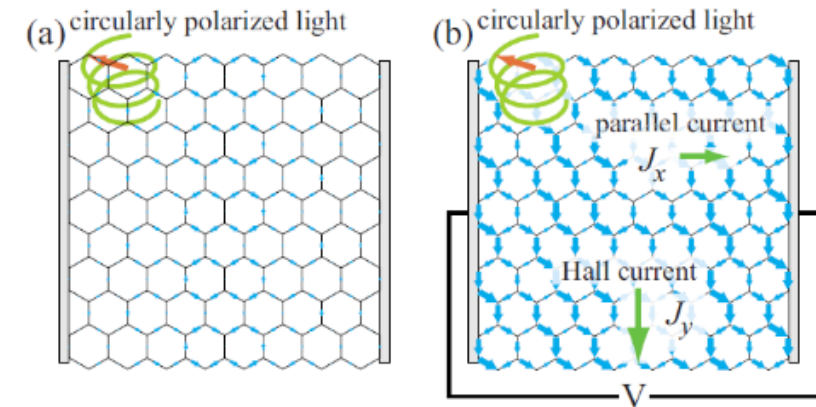
- Let us see the consequence by calculating σ_{yx}^C or σ_{yx}^S , which shows how a charge or spin current flows in $\parallel y$ when the probe field is applied in $\parallel x$.
- **CP** light causes the anomalous Hall effect ($\sigma_{yx}^C = -\sigma_{xy}^C \neq 0$).

T. Oka and H. Aoki, Phys. Rev. B 79, 081406(R) (2009).

When the helicity of CP light is changed, the sign of σ_{yx}^C is reversed: **time-reversal symmetry is broken.**

Onsager reciprocal relations

$$\begin{aligned} \sigma_{yx}^C(\mathbf{H}) &= \sigma_{xy}^C(-\mathbf{H}) & \sigma_{yx}^C[\mathbf{A}_{\text{LCP}}(t)] &= \sigma_{xy}^C[\mathbf{A}_{\text{LCP}}(-t)] \\ \sigma_{xy}^C(-\mathbf{H}) &= -\sigma_{xy}^C(\mathbf{H}) & &= \sigma_{xy}^C[\mathbf{A}_{\text{RCP}}(t)] \\ \therefore \sigma_{yx}^C(\mathbf{H}) &= -\sigma_{xy}^C(\mathbf{H}) & &= -\sigma_{xy}^C[\mathbf{A}_{\text{LCP}}(t)] \\ & & \therefore \sigma_{yx}^C[\mathbf{A}_{\text{LCP}}(t)] &= -\sigma_{xy}^C[\mathbf{A}_{\text{LCP}}(t)] \end{aligned}$$



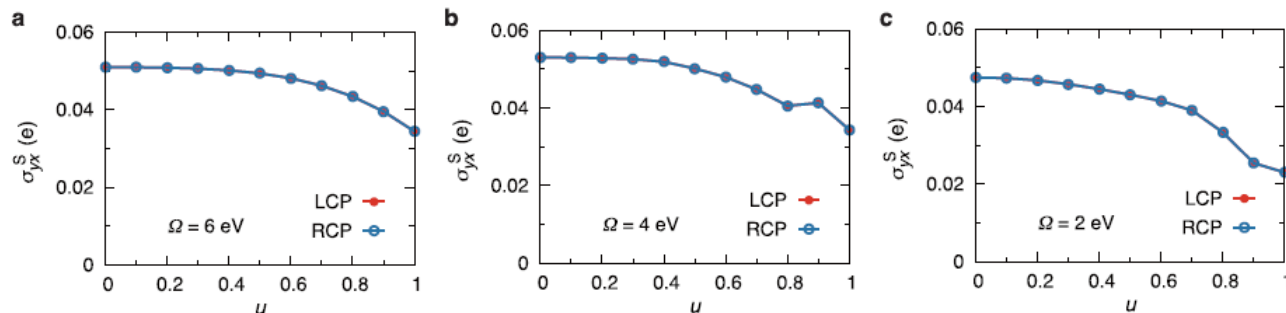
CP light:

It breaks time-reversal symmetry.

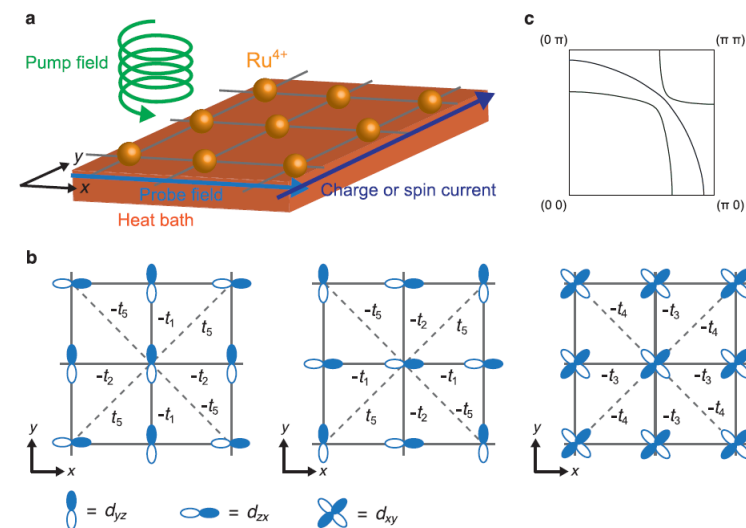
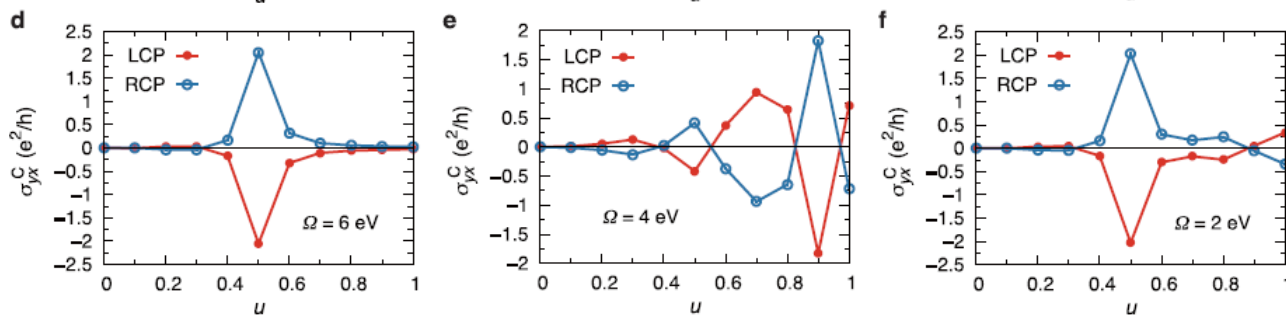
- How about the spin Hall effect (in multi-orbital Sr_2RuO_4 with strong SOC)

N. Arakawa and KY, Commun. Phys. 6, 43 (2023).

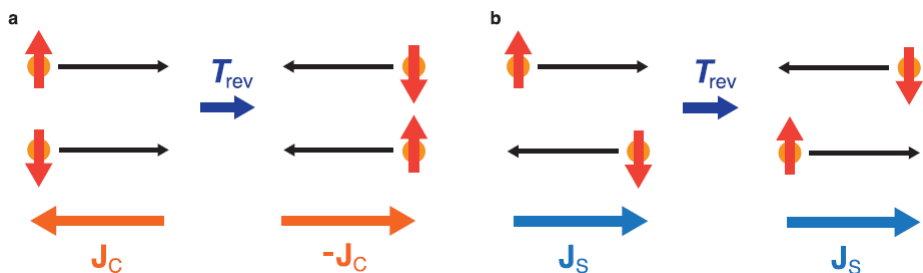
Spin Hall σ_{yx}^S



Anomalous Hall σ_{yx}^C



$$u = eA_0 = \frac{eE_0 a}{\hbar\Omega}$$



σ_{yx}^S is modulated by CP light.
The modulation is independent of the helicity of CP light because the spin current is unchanged by the time-reversal operation.

Model

- Pump-probe measurements of SHE or AHE

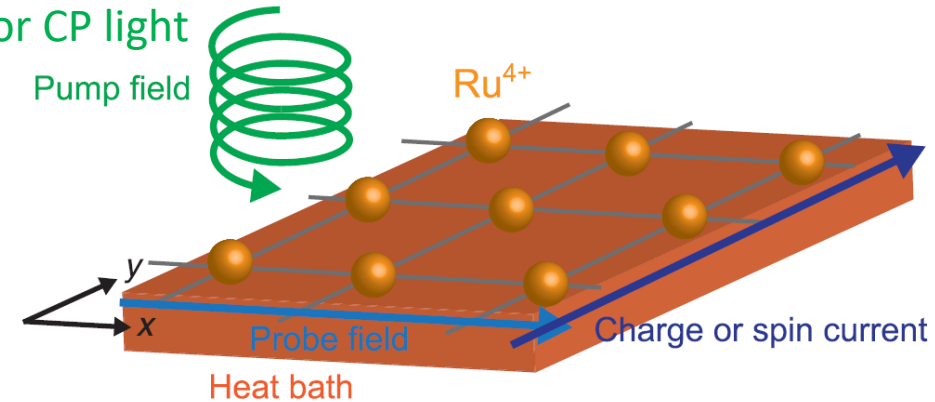
$$\mathbf{A}(t) = \mathbf{A}_{\text{pump}}(t) + \mathbf{A}_{\text{prob}}(t)$$

$$\mathbf{A}_{\text{pump}}(t) = {}^t(A_0 \cos \Omega t \ A_0 \sin(\Omega t + \delta)) \text{ for CP light}$$

$$\sigma_{yx}^{\text{Q}}(t, t') = \frac{1}{i\omega} \frac{\delta \langle j_{\text{Q}}^y(t) \rangle}{\delta A_{\text{prob}}^x(t')}$$

$$J_{\text{Q}}^y(t) = \sum_{\mathbf{k}} \sum_{a,b} \sum_{\sigma} v_{ab\sigma}^{(\text{Q})y}(\mathbf{k}, t) c_{\mathbf{k}a\sigma}^{\dagger}(t) c_{\mathbf{k}b\sigma}(t),$$

$$v_{ab\sigma}^{(\text{C})y}(\mathbf{k}, t) = (-e) \frac{\partial \epsilon_{ab}(\mathbf{k}, t)}{\partial k_y}, \quad v_{ab\sigma}^{(\text{S})y}(\mathbf{k}, t) = \frac{1}{2} \text{sgn}(\sigma) \frac{\partial \epsilon_{ab}(\mathbf{k}, t)}{\partial k_y}$$



Units: $\hbar = 1$, $k_{\text{B}} = 1$, and $a = 1$

Method

- Keldysh Green's function + Floquet representation

$$G = G_0 + G_0 \Sigma G \quad \text{Dyson's eq. (matrix form)}$$

$$G = \begin{pmatrix} G^R & G^K \\ 0 & G^A \end{pmatrix}, G_0 = \begin{pmatrix} G_0^R & G_0^K \\ 0 & G_0^A \end{pmatrix}, \Sigma = \begin{pmatrix} \Sigma^R & \Sigma^K \\ 0 & \Sigma^A \end{pmatrix}$$

Coupling to heat bath

$$G_{a\sigma b\sigma';n}^r(\mathbf{k}; \omega) = \int_{-\infty}^{\infty} dt_{\text{rel}} e^{i\omega t_{\text{rel}}} \int_0^T \frac{dt_{\text{av}}}{T} e^{in\Omega t_{\text{av}}} G_{a\sigma b\sigma'}^r(\mathbf{k}; t, t')$$

Wigner rep.

$$t_{\text{rel}} = t - t', \quad t_{\text{av}} = \frac{t + t'}{2}$$

$$[G_{a\sigma b\sigma'}^r(\mathbf{k}; \omega)]_{mn} = G_{a\sigma b\sigma';m-n}^r(\mathbf{k}; \omega + \frac{m+n}{2}\Omega) \quad \text{Floquet rep.}$$

Analytic results

- Time-averaged ~~Hall~~ ^{off-diagonal} conductivities

Hall if $\sigma_{yx}^C = -\sigma_{xy}^C$
OK for CPL

$$\begin{aligned} \sigma_{yx}^Q &= \lim_{\omega \rightarrow 0} \operatorname{Re} \int_0^T \frac{dt_{\text{av}}}{T} \int_{-\infty}^{\infty} dt_{\text{rel}} e^{i\omega t_{\text{rel}}} \sigma_{yx}^Q(t, t') \\ &= \frac{1}{N} \sum_{\mathbf{k}} \sum_{a,b,c,d} \sum_{\sigma,\sigma'} \int_{-\Omega/2}^{\Omega/2} \frac{d\omega'}{2\pi} \sum_{m,l,n,q=-\infty}^{\infty} [v_{ab\sigma}^{(Q)y}(\mathbf{k})]_{ml} \\ &\quad \times [v_{cd\sigma'}^{(C)x}(\mathbf{k})]_{nq} \left\{ \frac{\partial [G_{b\sigma c\sigma'}^R(\mathbf{k}, \omega')]_{ln}}{\partial \omega'} [G_{d\sigma' a\sigma}^<(\mathbf{k}, \omega')]_{qm} \right. \\ &\quad \left. - [G_{b\sigma c\sigma'}^<(\mathbf{k}, \omega')]_{ln} \frac{\partial [G_{d\sigma' a\sigma}^A(\mathbf{k}, \omega')]_{qm}}{\partial \omega'} \right\} \end{aligned}$$

$$G^< = \frac{1}{2}(G^K - G^R + G^A)$$

$$[v_{ab\sigma}^{(Q)\nu}(\mathbf{k})]_{mn} = \int_0^T \frac{dt}{T} e^{i(m-n)\Omega t} v_{ab\sigma}^{(Q)\nu}(\mathbf{k}, t)$$

Bicircular (BC) light:

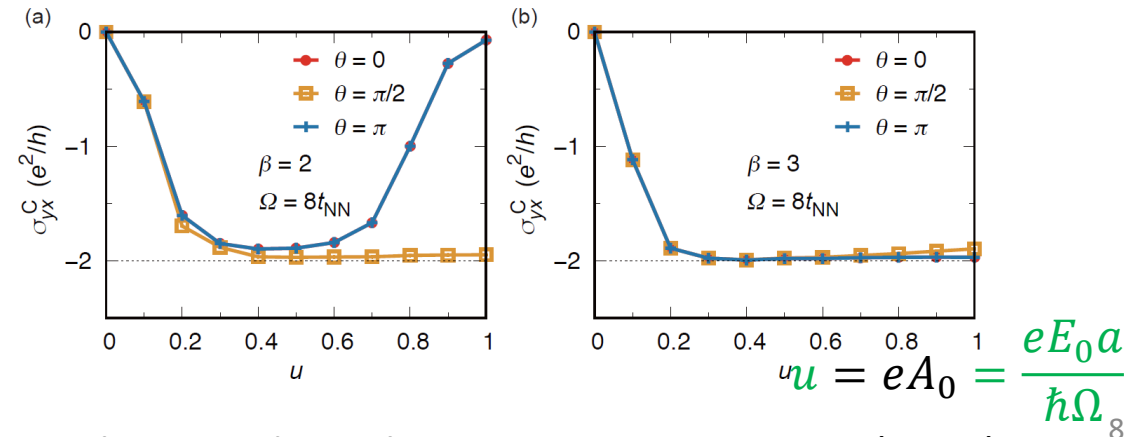
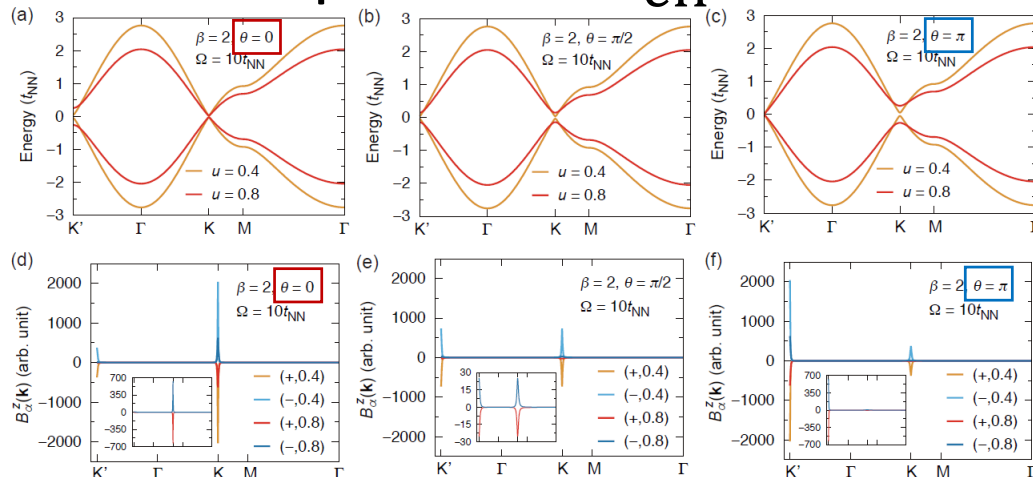
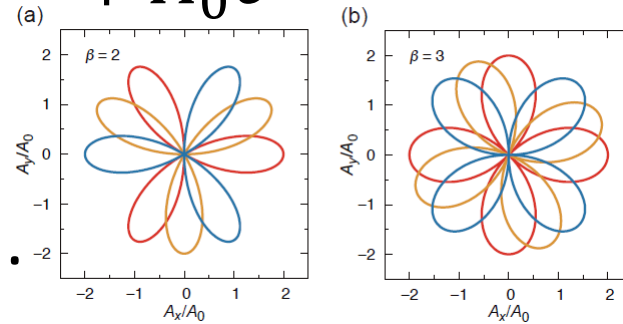
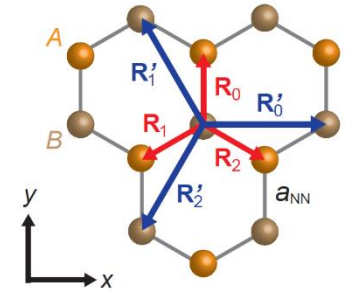
it consists of L&R-handed CP light w/ freq. Ω & $\beta\Omega$ and phase diff. θ , $A_x(t) + iA_y(t) = A_0 e^{i\Omega t} + A_0 e^{-i(\beta\Omega t - \theta)}$

- BC light breaks time-rev. sym. at least.

- It also breaks inversion sym. dep. on β & θ .

- $\beta = 2$ has a trefoil field. (even β has odd # of leaves in the trajectory)

- When graphene is irradiated by BC light, the valley degeneracy at **K and K'** is lifted for $\beta = 2$ and $\theta = 0, \pi$, leading to disproportionate Berry curvatures at K and K' points in H_{eff} and a valley-selective Hall effect.

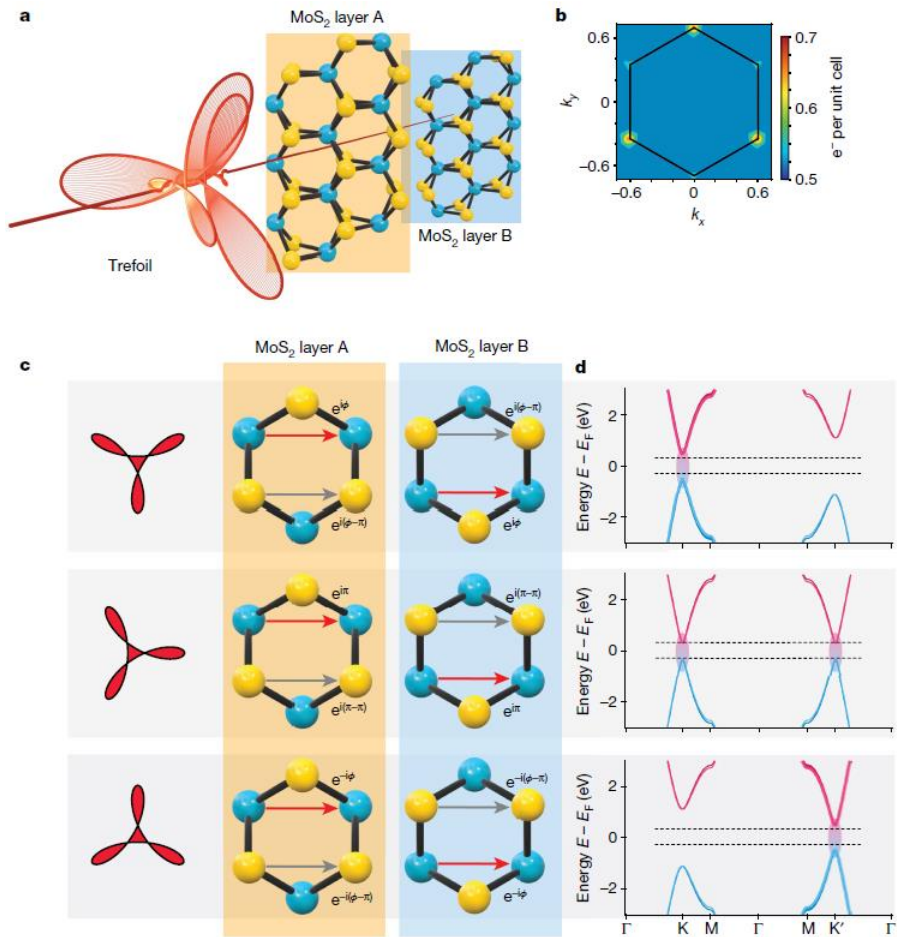


N. Arakawa and KY, Phys. Rev. B **109**, L241201 (2024).

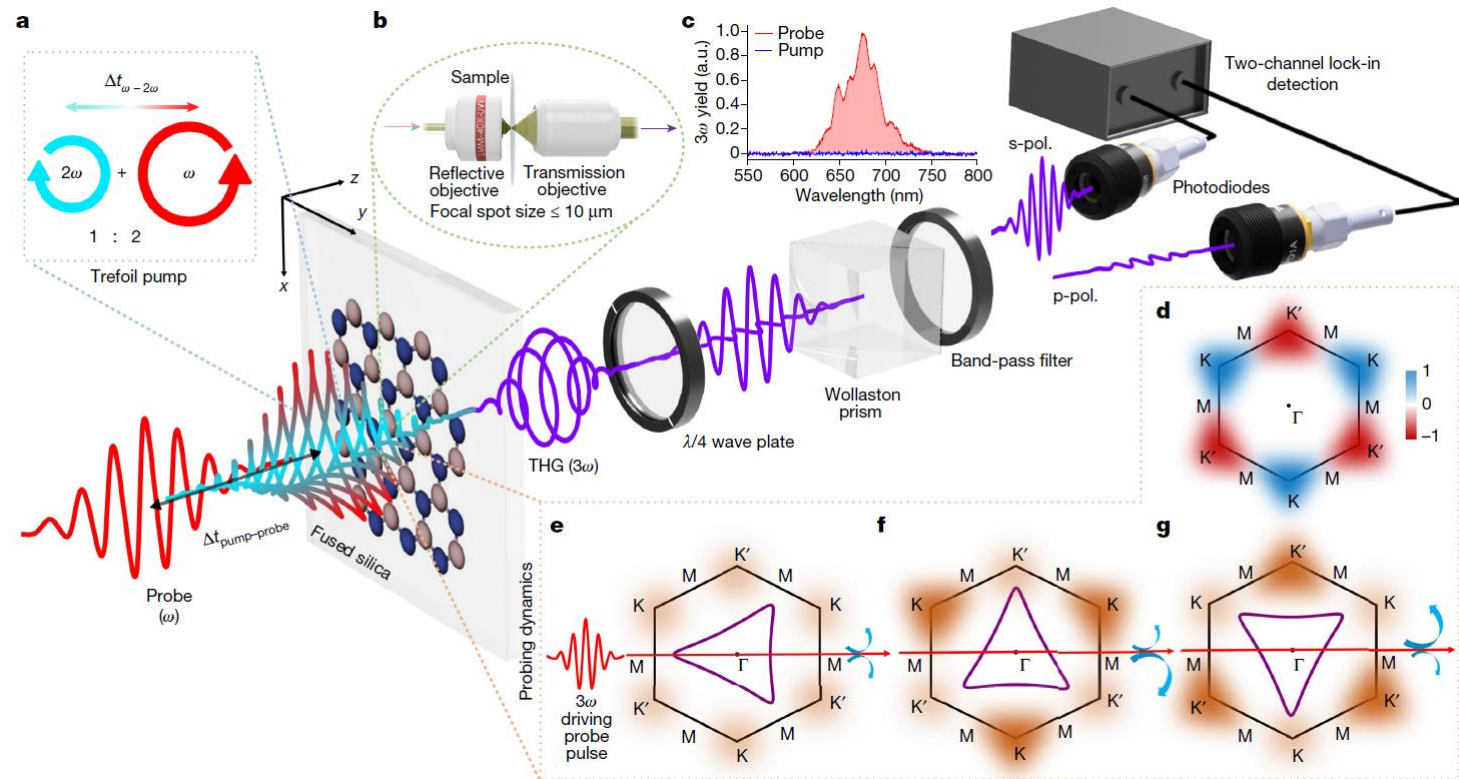
$$\nu u = eA_0 = \frac{eE_0 a}{\hbar\Omega} \quad 8$$

Recently, trefoil ($\beta = 2$) fields shown to induce valley pol.

Igor Tyulnev et al.,
 "Valleytronics in bulk MoS₂ with a topologic optical field,"
 Nature 628, 746 (2024).

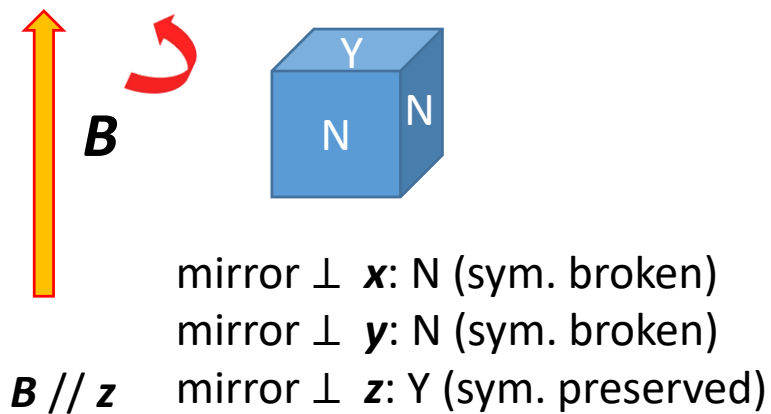


Sambit Mitra et al.,
 "Light-wave-controlled Haldane model in monolayer hexagonal boron nitride"
 Nature 628, 752 (2024).



So far, breaking of time-reversal & inversion symmetry is treated. Then, how about that of **mirror (reflection) symmetry**?

- Mirror symmetry is relevant to off-diagonal (transverse) conductivity including the Hall and anomalous Hall effects.



M. Naka, Y. Motome, and H. Seo, PRB 106, 195149 (2022).
 “Anomalous Hall effect in antiferromagnetic perovskites”

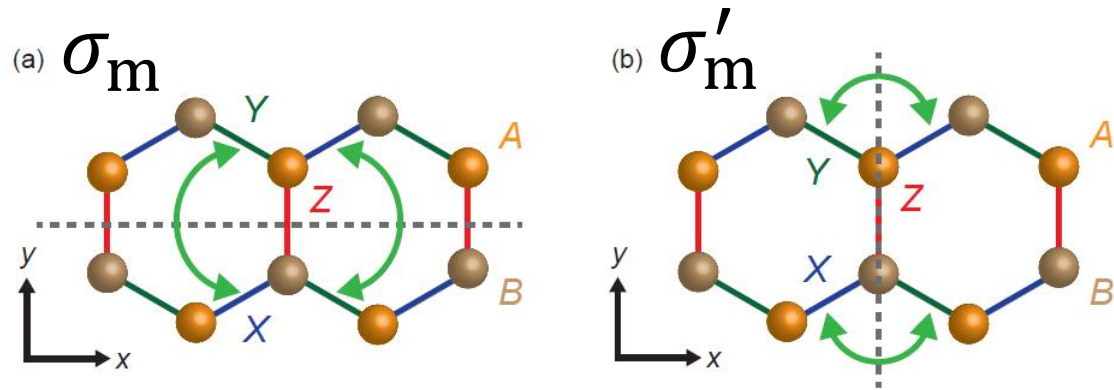
TABLE I. Relation between the AHE and the symmetries of the AFM patterns on $Pbnm$ structure. Y (N) represents the presence (absence) of the symmetry.

AFM	mirror $\perp z$	b -glide $\perp x$	n -glide $\perp y$	active AHE
$C_x F_y A_z$	N	N	Y	σ_{xz}
$F_x C_y G_z$	N	Y	N	σ_{yz}
$G_x A_y F_z$	Y	N	N	σ_{xy}
$A_x G_y C_z$	Y	Y	Y	N/A

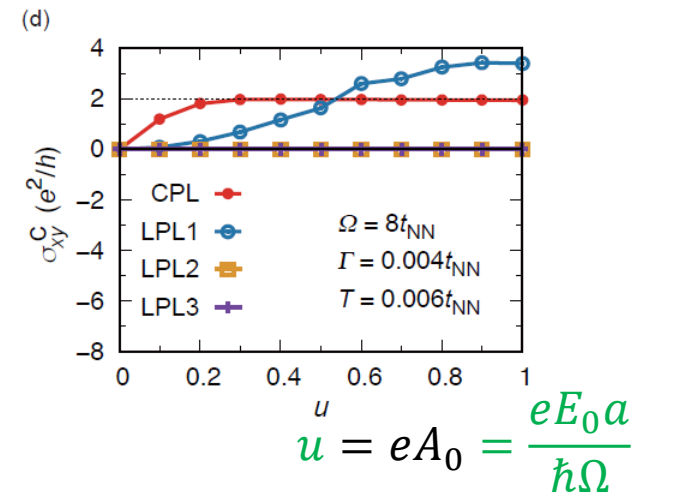
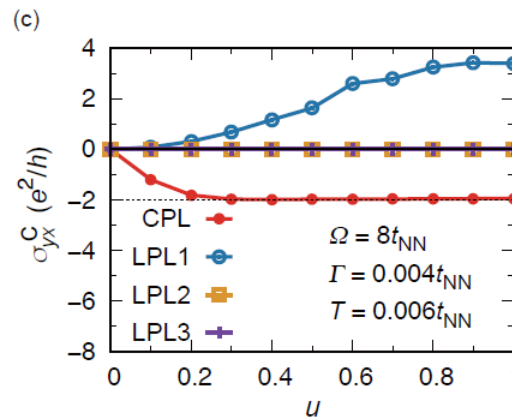
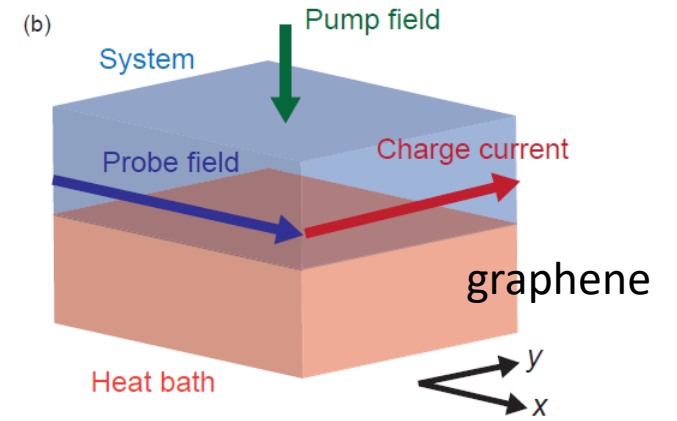
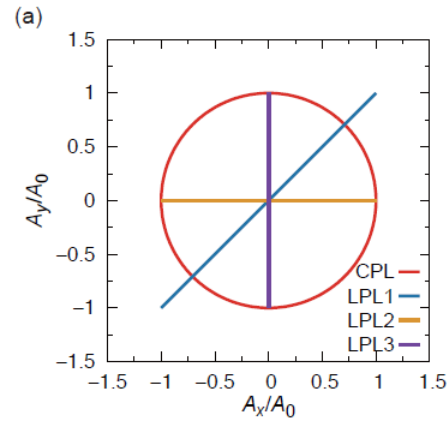
glide (=reflection + translation) \sim mirror (=reflection)

Which mirror (glide) symmetry is broken is important for $\sigma_{ij} \neq 0$ with particular ij .

In addition to CP, we consider the breaking of mirror symmetry, keeping time-reversal sym., i.e., **LP** light w/ polarization not \parallel, \perp the mirror plane.



	CPL	LPL1	LPL2	LPL3	
T_{rev}	Broken	Preserved	Preserved	Preserved	
σ_m	Broken	Broken	Preserved	Broken	
$\sigma_m T_t$	Broken	Broken	Preserved	Preserved	$T_t : t \rightarrow t - \frac{\pi}{\Omega}$
σ'_m	Broken	Broken	Broken	Preserved	
$\sigma'_m T_t$	Broken	Broken	Preserved	Preserved	$T_t : t \rightarrow t - \frac{\pi}{\Omega}$
C_3	Broken	Broken	Broken	Broken	
$C_3 T_t$	Preserved	Broken	Broken	Broken	$T_t : t \rightarrow t + \frac{2\pi}{3\Omega}$
σ_{yx}^C	Antisymmetric	Symmetric	Vanishing	Vanishing	



N. Arakawa and KY, J. Phys. Soc. Jpn. 93, 084701 (2024).

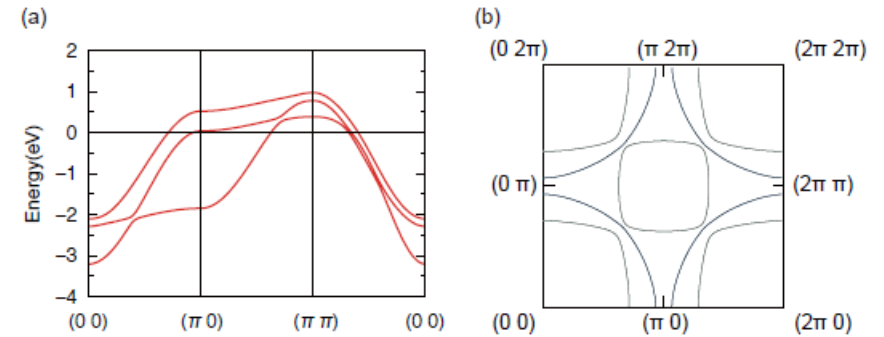
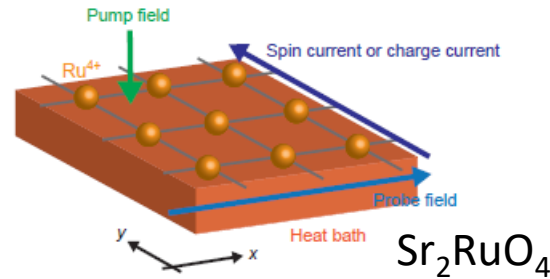
- **LP** light can break mirror symmetry, depending on its polarization, and lead to nonzero σ_{yx}^C , which is not a Hall effect since $\sigma_{yx}^C = \sigma_{xy}^C$ (time-reversal symmetry is preserved).

Bicircular (BC) light again:

$$A_x(t) + iA_y(t) = A_0 e^{i\Omega t} + A_0 e^{-i(\beta\Omega t - \theta)}$$

- The trajectory of $A(t)$ can break mirror symmetry, depending on θ .

N. Arakawa and KY, in preparation

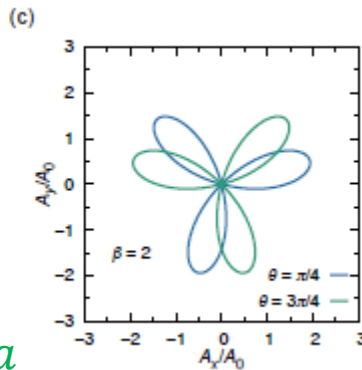
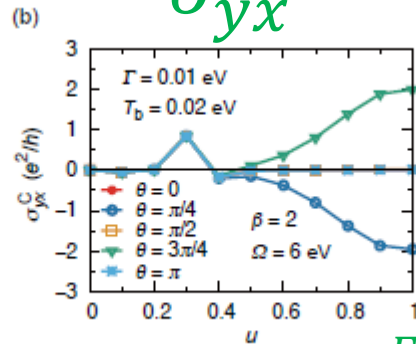
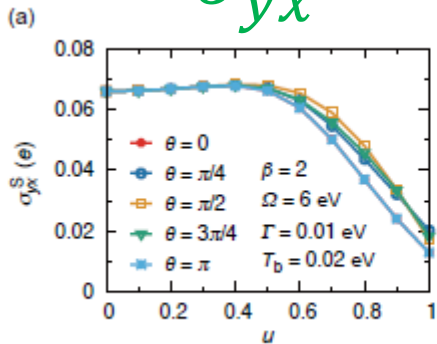


Spin Hall

$$\sigma_{yx}^S$$

Anomalous Hall

$$\sigma_{yx}^C$$



$$u = eA_0 = \frac{eE_0 a}{\hbar\Omega}$$

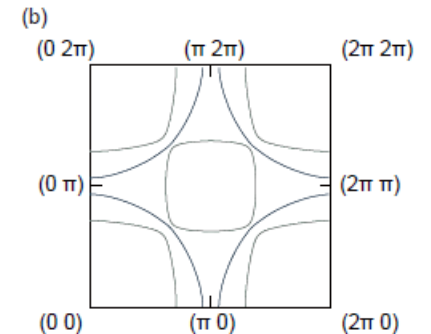
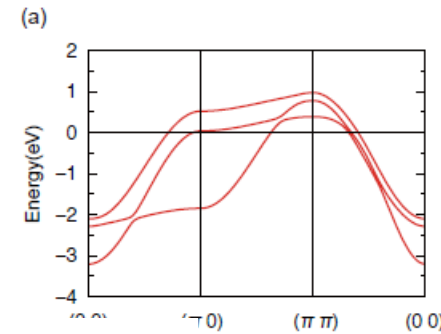
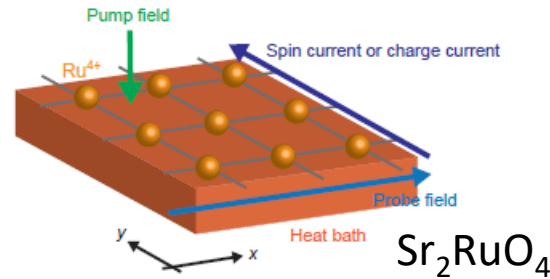
If a mirror operation for θ gives the trajectory for θ_M , σ_{yx}^C for θ and σ_{yx}^C for θ_M are of opposite signs and almost the same magnitude for moderately large field strengths u . 12

Bicircular (BC) light again:

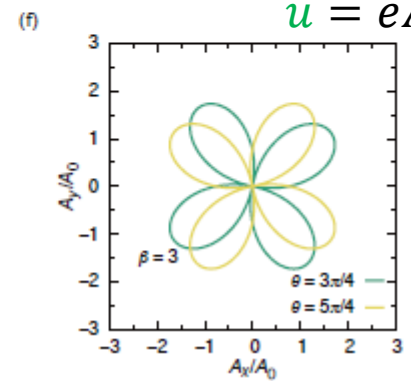
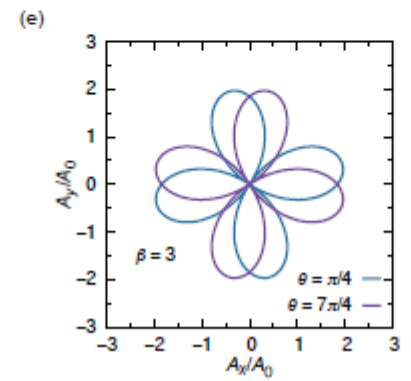
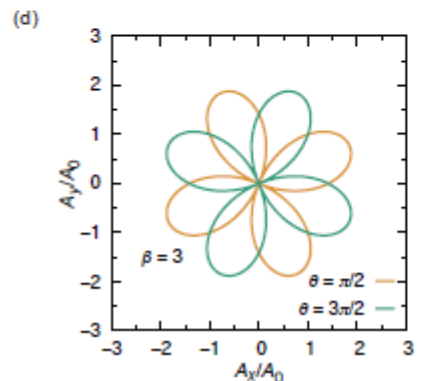
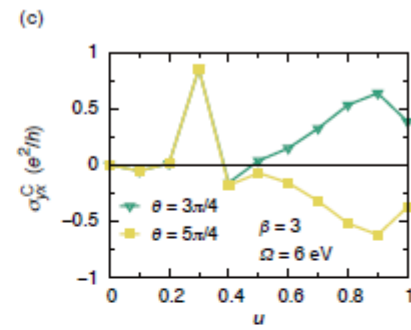
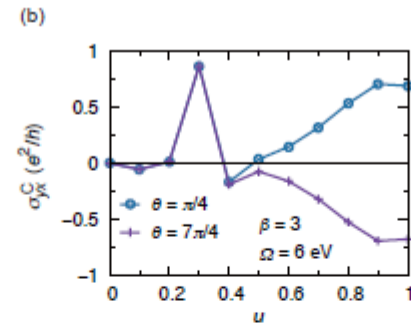
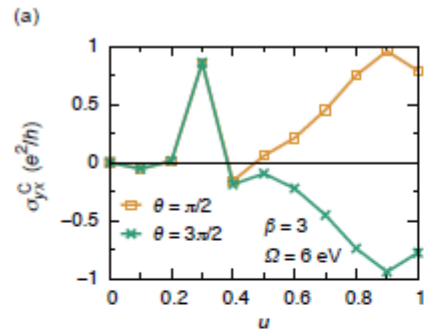
$$A_x(t) + iA_y(t) = A_0 e^{i\Omega t} + A_0 e^{-i(\beta\Omega t - \theta)}$$

- The trajectory of $\mathbf{A}(t)$ can break mirror symmetry, depending on θ .

N. Arakawa and KY, in preparation



Anomalous Hall
 σ_{yx}^C



$$u = eA_0 = \frac{eE_0 a}{\hbar\Omega}$$

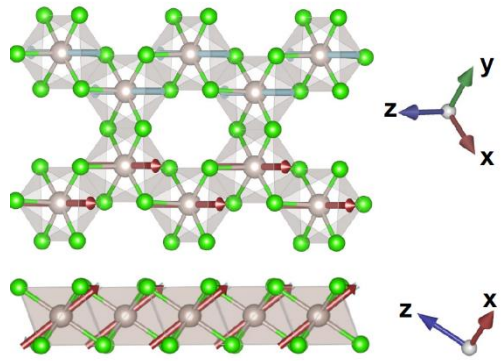
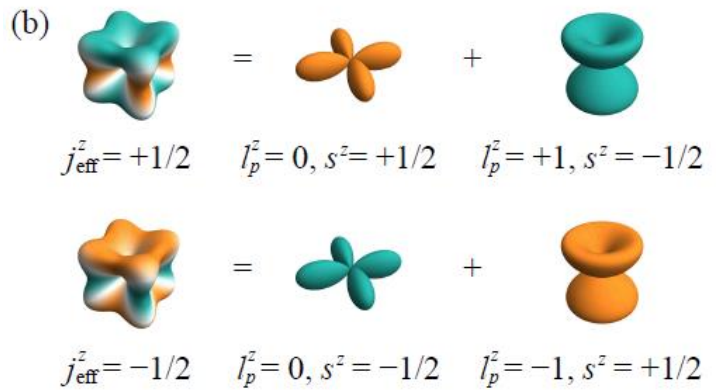
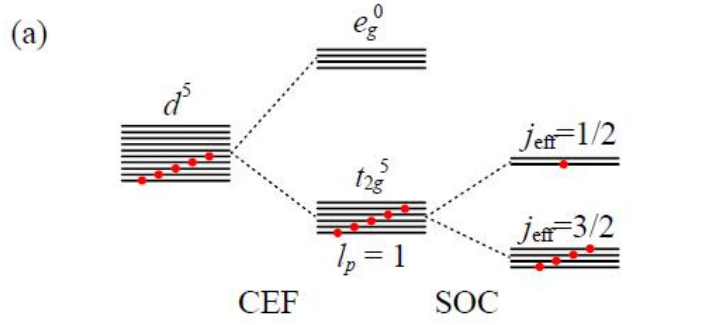
Summary 1:

- Linearly pol. (LP) light can break mirror sym.: $\sigma_{yx}^C = \sigma_{xy}^C \neq 0$ (not Hall)
- Circularly pol. (CP) light breaks time-rev. sym.: $\sigma_{yx}^C = -\sigma_{xy}^C \neq 0$, inverse Faraday, etc.
- Bicircular (BC) light can break time-rev. and inv. sym.: valley-selective Hall, valley pol. etc.

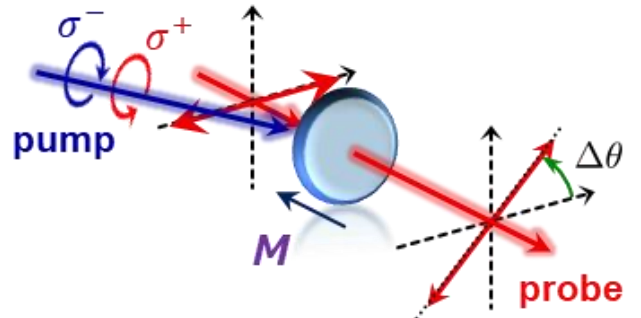
or

time-rev. and mirror sym.: θ -sensitive σ_{yx}^C for $\frac{eE_0a}{\hbar\Omega} \sim 1$

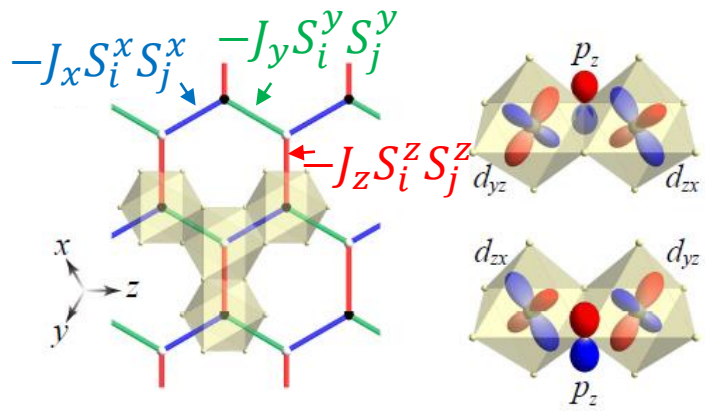
Photoinduced magnetization in quantum spin-liquid α -RuCl₃



S. M. Winter et al., PRB 2016



T. Amano, KY, S. Iwai et al., Phys. Rev. Res. 4, L032032 (2022).

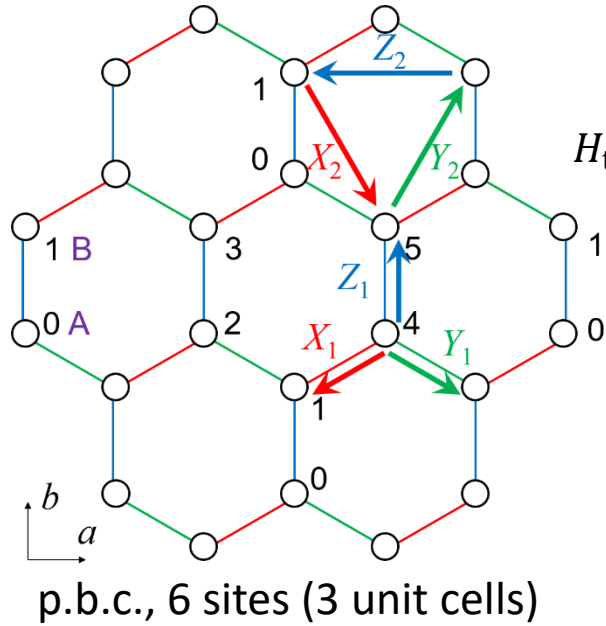


Y. Motome and J. Nasu, JPSJ 2020

- Theories
 - A. Kitaev, Ann. Phys. 321, 2 (2006)
 - G. Jackeli and G. Khaliullin, PRL 102, 017205 (2009)
 - H.-S. Kim and H.-Y. Kee, PRB 93, 155143 (2016).
 - S. M. Winter et al., PRB 93, 214431 (2016).
- Experiments
 - L. J. Sandilands et al., PRB 93, 075144 (2016).
 - L. J. Sandilands et al., PRB 94, 195156 (2016).
 - P. Warzanowski et al., PRR 2, 042007(R) (2020).

Three-orbital Hubbard model for Kitaev materials

S. M. Winter, Y. Li, H. O. Jeschke, and Roser Valentí, PRB2016



$$H_{\text{tot}} = H_{\text{hop}} + H_{\text{CF}} + H_{\text{SO}} + H_U$$

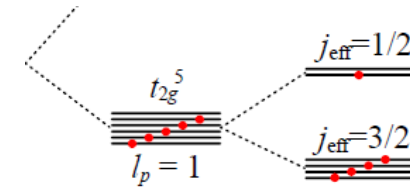
$$H_{\text{hop}} = - \sum_{ij} \vec{c}_i^\dagger \{ \mathbf{T}_{ij} \otimes \mathbb{I}_{2 \times 2} \} \vec{c}_j \quad \vec{c}_i^\dagger = (c_{i,yz,\uparrow}^\dagger, c_{i,yz,\downarrow}^\dagger, c_{i,xz,\uparrow}^\dagger, c_{i,xz,\downarrow}^\dagger, c_{i,xy,\uparrow}^\dagger, c_{i,xy,\downarrow}^\dagger)$$

(hole picture)

$$\mathbf{T}_1^X = \begin{pmatrix} t_3 & t_4 & t_4 \\ t_4 & t_1 & t_2 \\ t_4 & t_2 & t_1 \end{pmatrix} \quad \mathbf{T}_1^Y = \begin{pmatrix} t_1 & t_4 & t_2 \\ t_4 & t_3 & t_4 \\ t_2 & t_4 & t_1 \end{pmatrix} \quad \mathbf{T}_1^Z = \begin{pmatrix} t_1 & t_2 & t_4 \\ t_2 & t_1 & t_4 \\ t_4 & t_4 & t_3 \end{pmatrix}$$

$$H_{\text{SO}} = \frac{\lambda}{2} \sum_i \vec{c}_i^\dagger \begin{pmatrix} 0 & -i\sigma_z & i\sigma_y \\ i\sigma_z & 0 & -i\sigma_x \\ -i\sigma_y & i\sigma_x & 0 \end{pmatrix} \vec{c}_i$$

$$H_U = U, U', J_H \text{ terms} \quad U' = U - 2J_H$$



CEF SOC
Y. Motome and J. Nasu, JPSJ 2020

$J_{\text{eff}} = \frac{1}{2}$: half filled

$$\left| \frac{1}{2}, \frac{1}{2} \right\rangle = p_\uparrow^\dagger |0\rangle \equiv \frac{1}{\sqrt{3}} (-c_{xy,\uparrow}^\dagger - ic_{xz,\downarrow}^\dagger - c_{yz,\downarrow}^\dagger) |0\rangle$$

$$\left| \frac{1}{2}, -\frac{1}{2} \right\rangle = p_\downarrow^\dagger |0\rangle \equiv \frac{1}{\sqrt{3}} (c_{xy,\downarrow}^\dagger + ic_{xz,\uparrow}^\dagger - c_{yz,\uparrow}^\dagger) |0\rangle$$

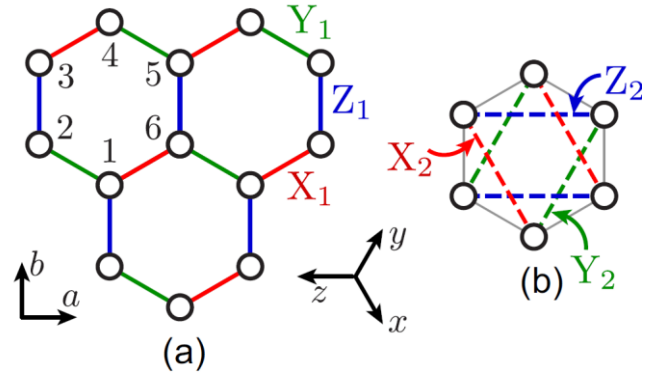
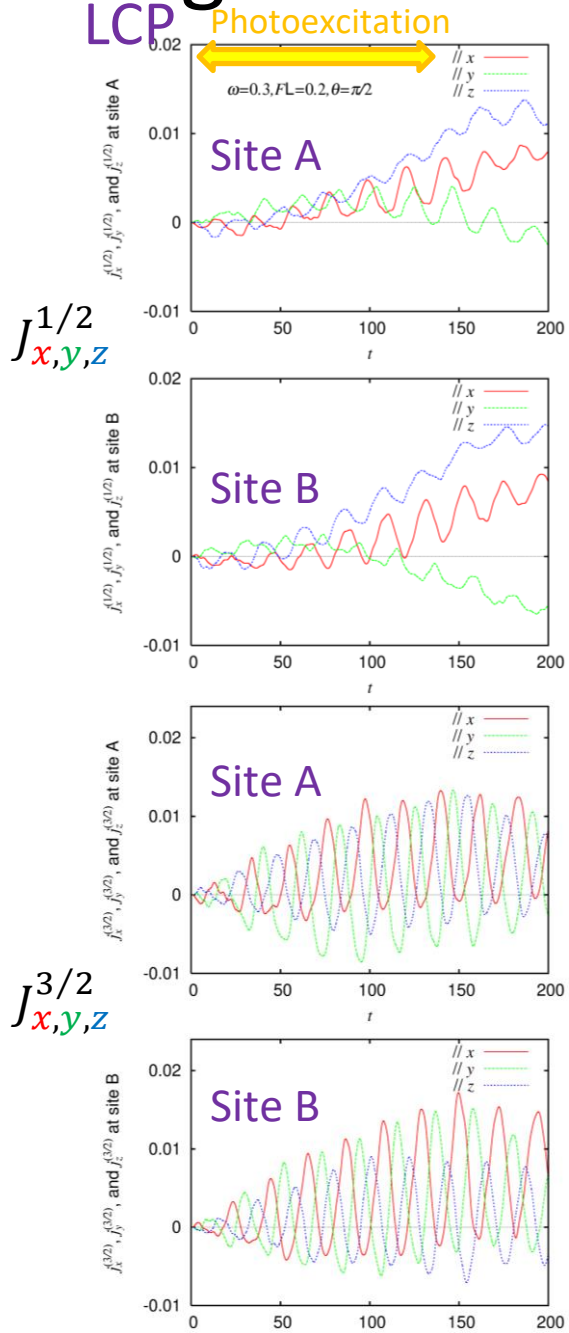
$$m_x^{(1/2)} \equiv \frac{1}{2} (p_\uparrow^\dagger p_\downarrow + p_\downarrow^\dagger p_\uparrow)$$

$$m_y^{(1/2)} \equiv \frac{1}{2} (-ip_\uparrow^\dagger p_\downarrow + ip_\downarrow^\dagger p_\uparrow)$$

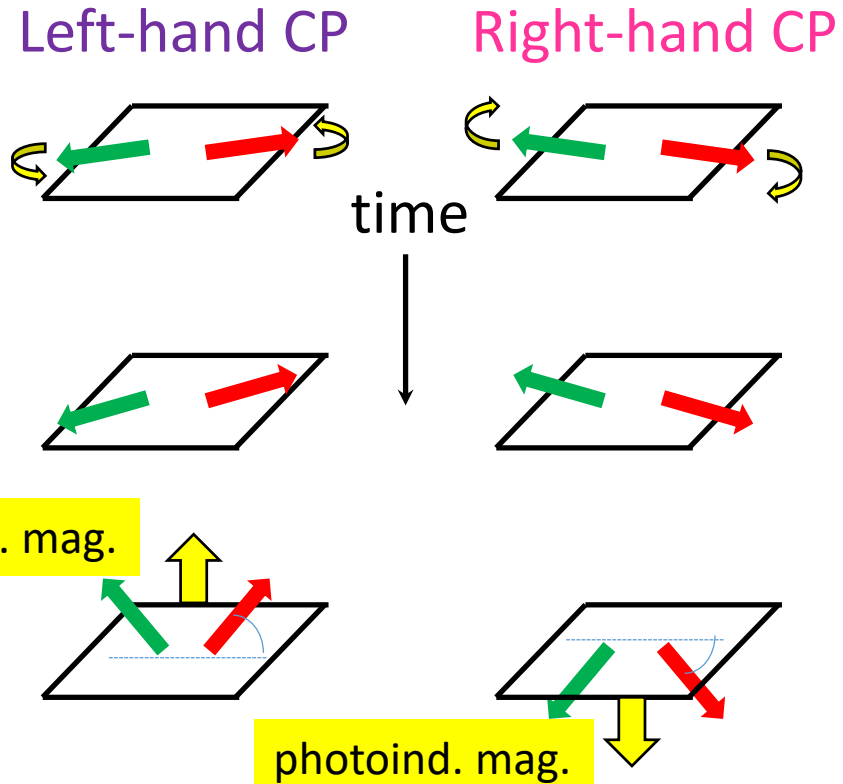
$$m_z^{(1/2)} \equiv \frac{1}{2} (p_\uparrow^\dagger p_\uparrow - p_\downarrow^\dagger p_\downarrow)$$

$$m_\perp^{(1/2)} \equiv \frac{1}{\sqrt{3}} (m_x^{(1/2)} + m_y^{(1/2)} + m_z^{(1/2)})$$

Magnetization dynamics induced by circularly polarized light

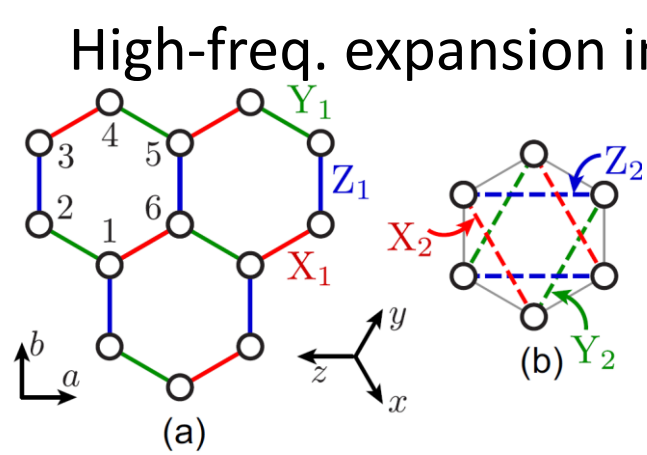
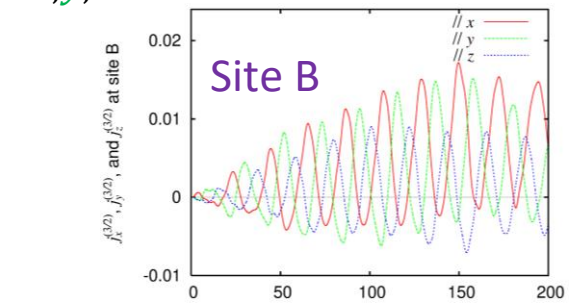
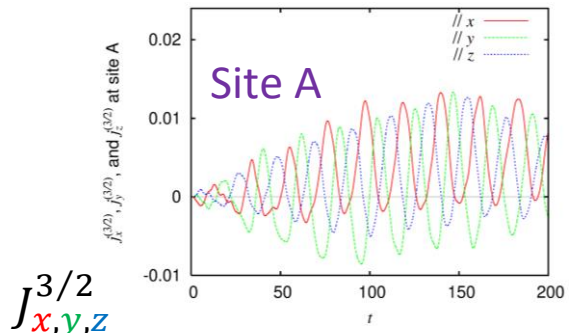
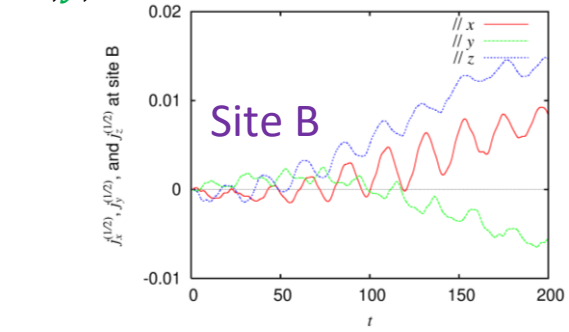
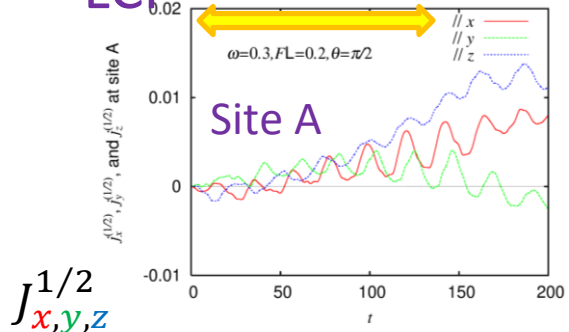


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Magnetization dynamics induced by circularly polarized light

LCP Photoexcitation



High-freq. expansion in Floquet theory: $H_F^{(2)}$

$$H_F^{(2)} = \sum_{m>0} \frac{[H_m, H_{-m}]}{m\hbar\omega}$$

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$$H_F^{(2)} \simeq \frac{1}{\hbar\omega} \sum_{iab\sigma} J_1^2 \left(\frac{eaF_L}{\hbar\omega} \right) (2i) \sin \frac{2\pi}{3} ([T_1^Y, T_1^Z] + [T_1^Z, T_1^X] + [T_1^X, T_1^Y])_{ab} c_{i,a,\sigma}^\dagger c_{i,b,\sigma}$$

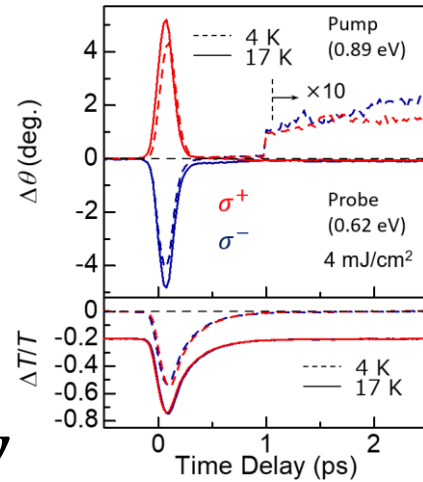
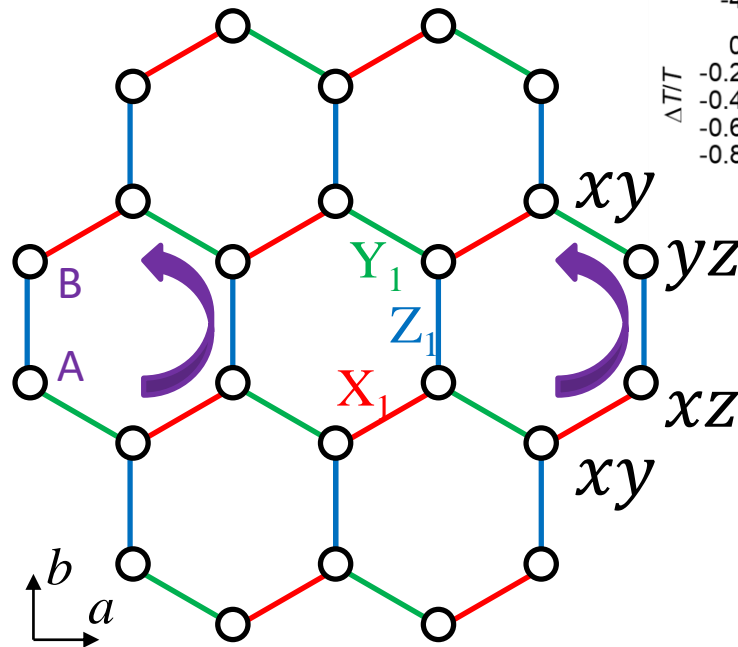
$$\simeq \frac{1}{\hbar\omega} J_1^2 \left(\frac{eaF_L}{\hbar\omega} \right) \sqrt{3} (t_2 - t_4) [t_2 - t_4 + 2(t_3 - t_1)] < 0 \text{ for L, } > 0 \text{ for R}$$

$$\times \sum_{i\sigma} \begin{pmatrix} c_{i,yz,\sigma}^\dagger & c_{i,xz,\sigma}^\dagger & c_{i,xy,\sigma}^\dagger \end{pmatrix} \begin{pmatrix} 0 & -i & i \\ i & 0 & -i \\ -i & i & 0 \end{pmatrix} \begin{pmatrix} c_{i,yz,\sigma} \\ c_{i,xz,\sigma} \\ c_{i,xy,\sigma} \end{pmatrix}$$

$$l_x = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{pmatrix}, \quad l_y = \begin{pmatrix} 0 & 0 & i \\ 0 & 0 & 0 \\ -i & 0 & 0 \end{pmatrix}, \quad l_z = \begin{pmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

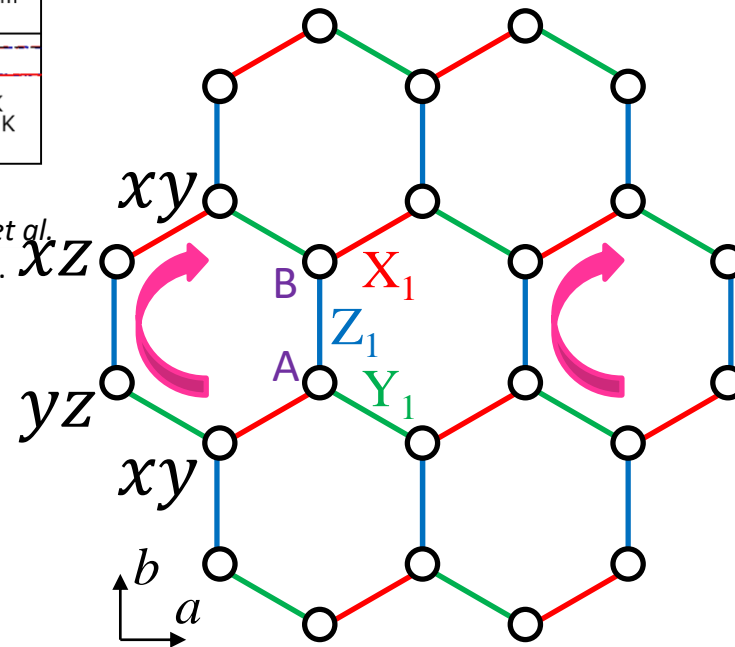
Emergence of angular momentum in multi-orbital systems

- Left-hand circular pol.



T. Amano, KY, S. Iwai *et al.*
Phys. Rev. Res. (2022).

- Right-hand circular pol.



- Main transitions when (interorbital) t_2 processes are dominant.

- Quantitatively, (intraorbital) t_3 processes are also important. $\mathbf{T}_1^Z = \begin{pmatrix} t_1 & t_2 & t_4 \\ t_2 & t_1 & t_4 \\ t_4 & t_4 & t_3 \end{pmatrix}$

Summary 2:

CP → effective mag. fields in multi-orb. systems

- Photoinduced magnetization in α -RuCl₃: explained by Floquet theory.
- $H_F^{(2)} = \sum_{m>0} \frac{[H_m, H_{-m}]}{m\hbar\omega}$ gives a helicity-dependent effective magnetic field on $l_{\text{eff}} \perp$ honeycomb plane.

T. Amano, KY, S. Iwai *et al.* Phys. Rev. Research 4, L032032 (2022).

KY, JPSJ 91, 104702 (2022).

Intersite interorbital hopping processes are essential.

Charge DOF in frustrating spin systems for emergent magnetization
in the spin-orbit assisted Mott insulator.

⇔ effective magnetic fields deep in the insulating phase.

A. Sriram and M. Claassen, Phys. Rev. Research 4, L032036 (2022),

S. Banerjee *et al.*, Phys. Rev. B 105, L180414 (2022).