



The importance of Shear in sliding CDW observed by Xfel source

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Transformations of Correlated Electronic States by Electric or Optical Impacts. International research school and workshop IMPACT – 2024

*August 19 – 31, 2024
Carg se, France*

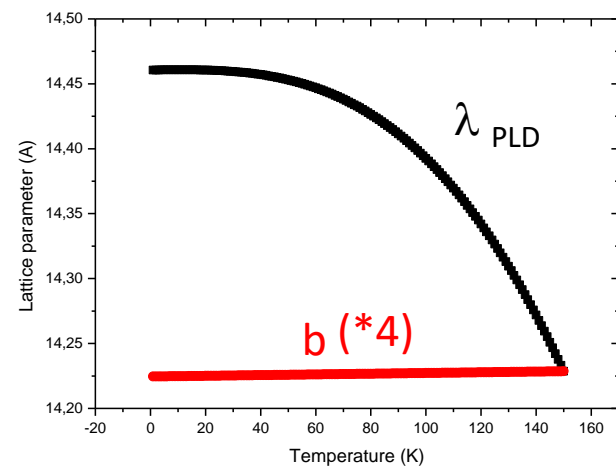
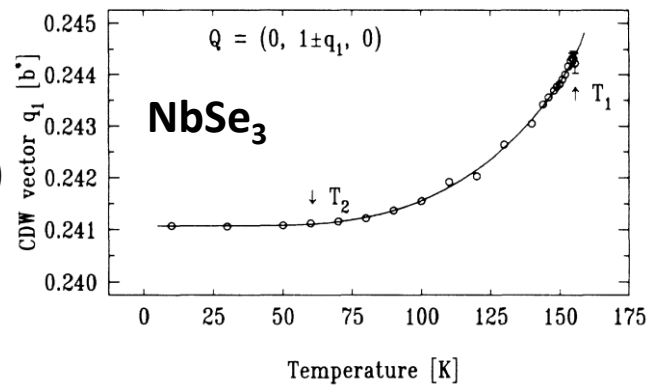


[Overview](#) [Accommodation](#) [Room Reservation](#) [Transportation](#) [Venue and location](#) [Program](#) [Registration and conference fee](#)

[Practical information](#) [Abstract submission.](#)

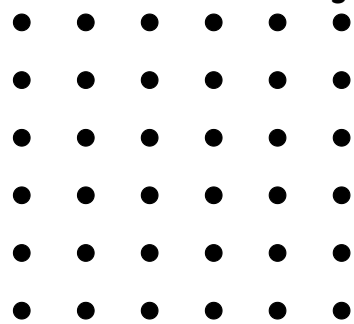
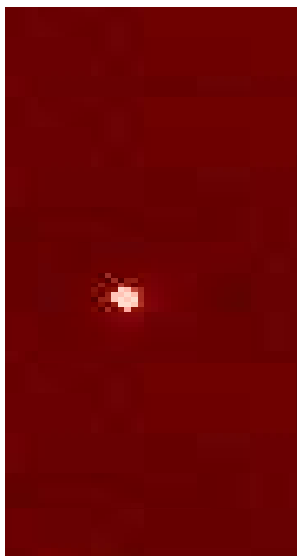
Incommensurate CDW is sensitive to numerous excitations

1. Temperature



Charge Density Wave

TbTe₃

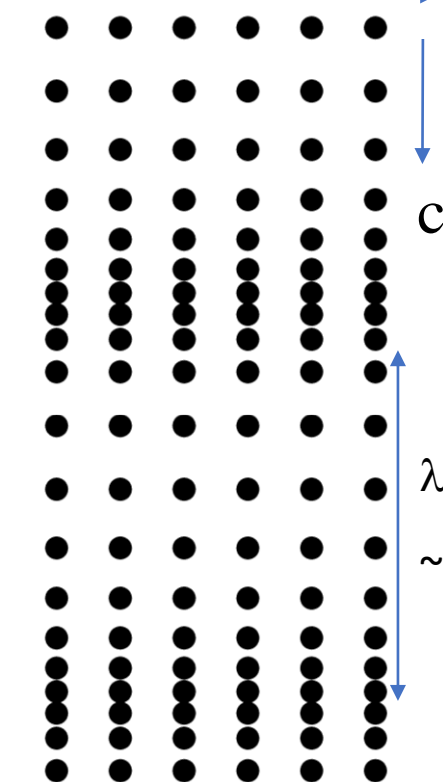
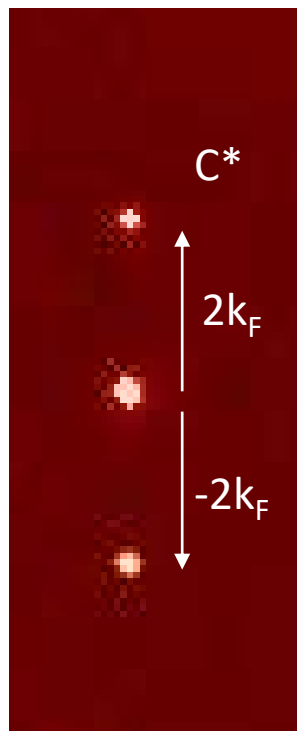


Electronic (metal-insulator)

+

structural

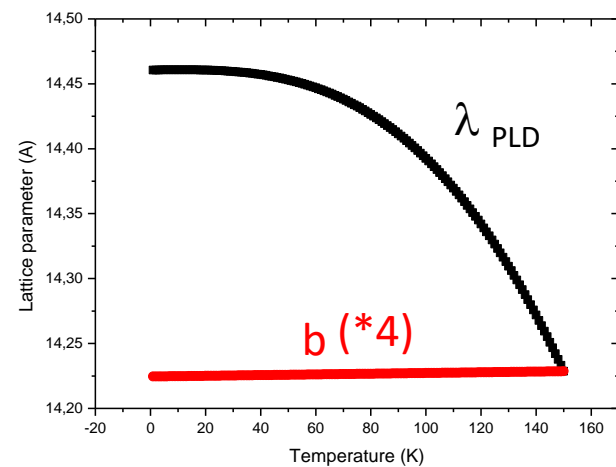
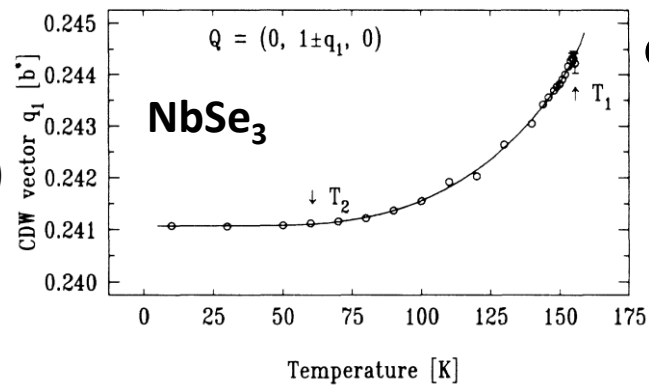
a



Incommensurate CDW is sensitive to numerous excitations

2. Ultra short light pulse

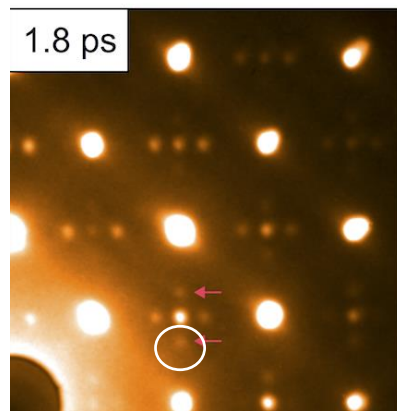
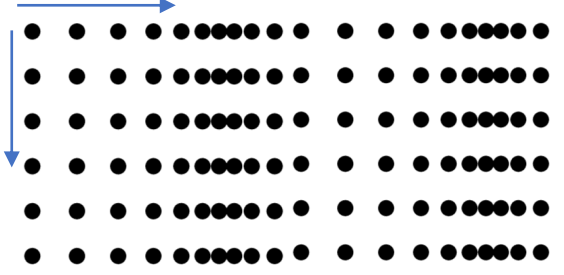
1. Temperature



a

LaTe₃

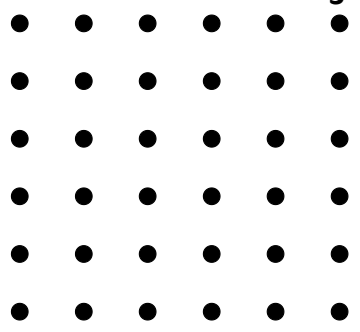
c



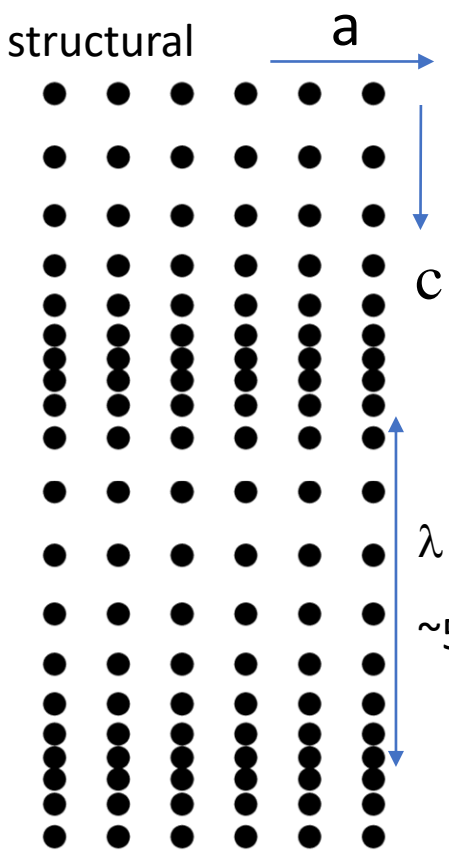
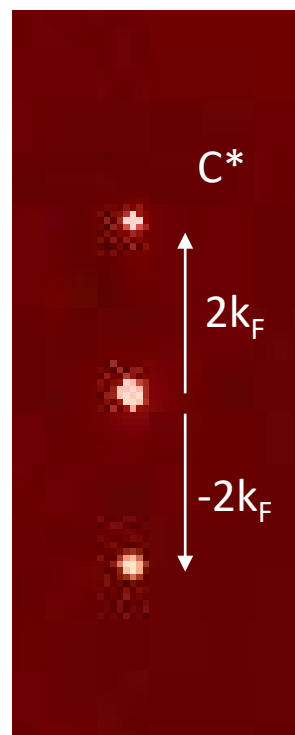
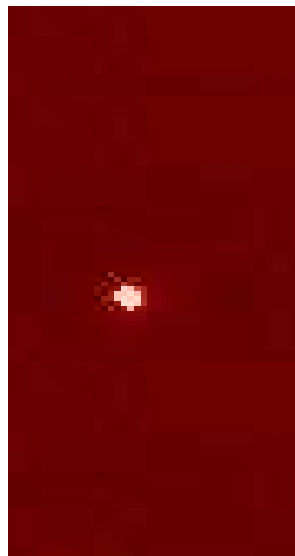
A. Kogar et al., Nat. Phys. **16**, 159 (2020)

Charge Density Wave

TbTe₃



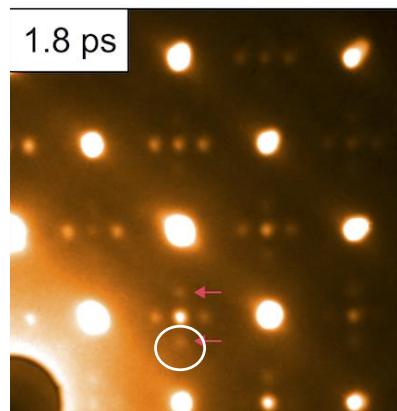
Electronic (metal-insulator)
 +
 structural



A.H. Moudden, PRL 1990

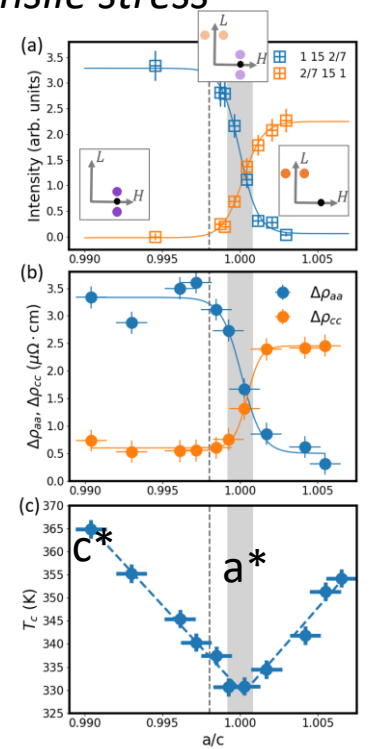
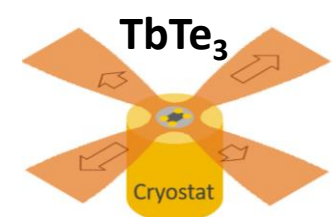
Incommensurate CDW is sensitive to numerous excitations

2. Ultra short light pulse



A. Kogar et al., Nat. Phys. **16**, 159 (2018)

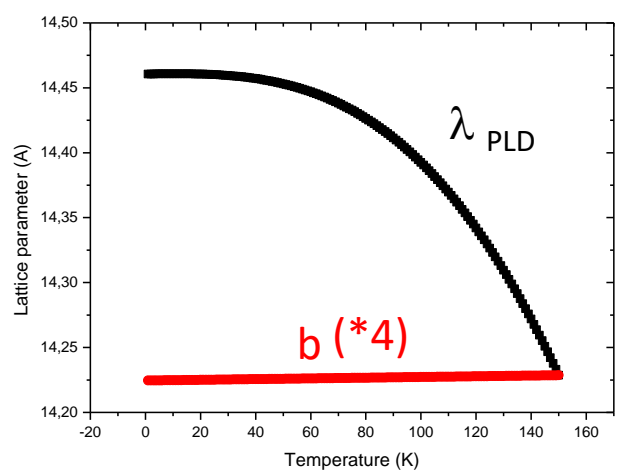
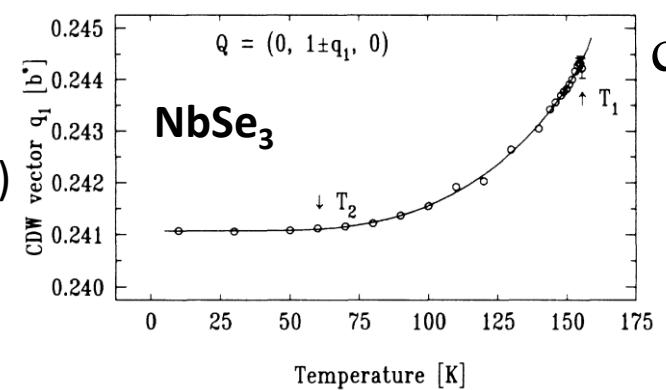
3. CDW tuned by biaxial tensile stress



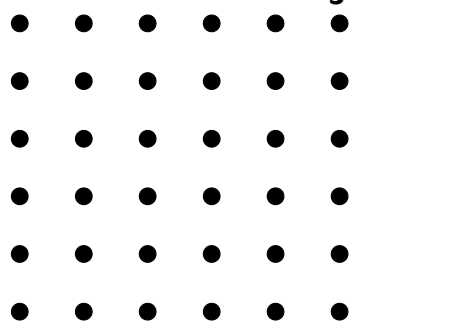
A. Gallo-Frantz et al., Nat. Comm.,

(V. Jacques presentation Last week)

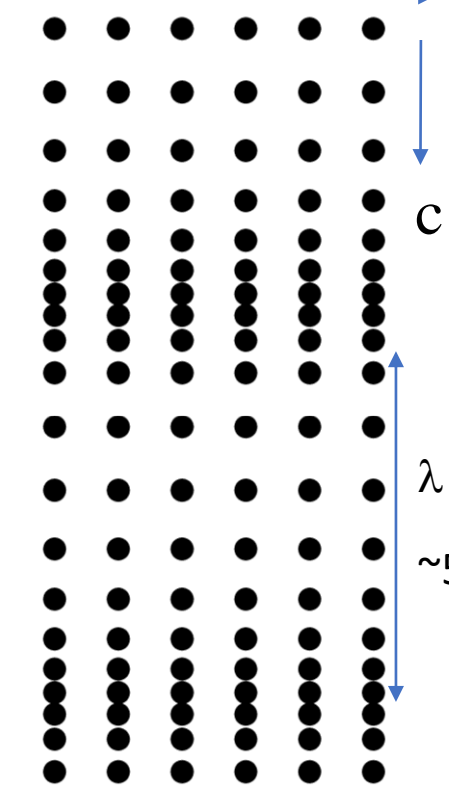
1. Temperature



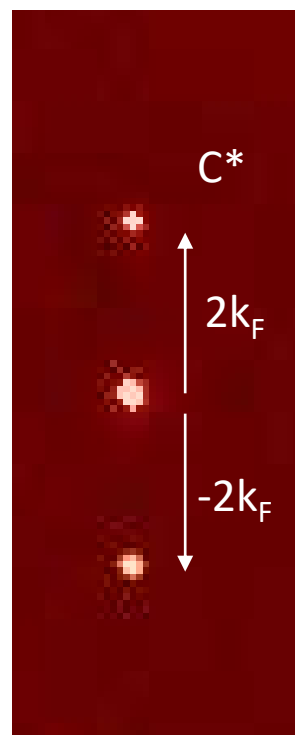
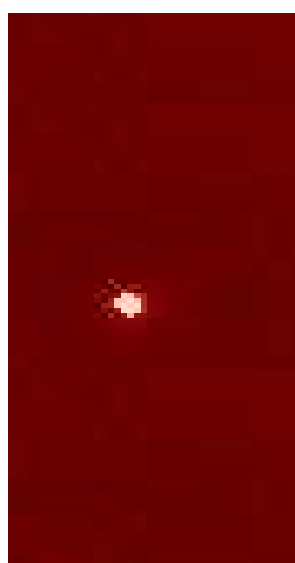
Charge Density Wave



Electronic (metal-insulator) + structural



A.H. Moudden, PRL 1990



c^*

$2k_F$

$-2k_F$

λ PLD

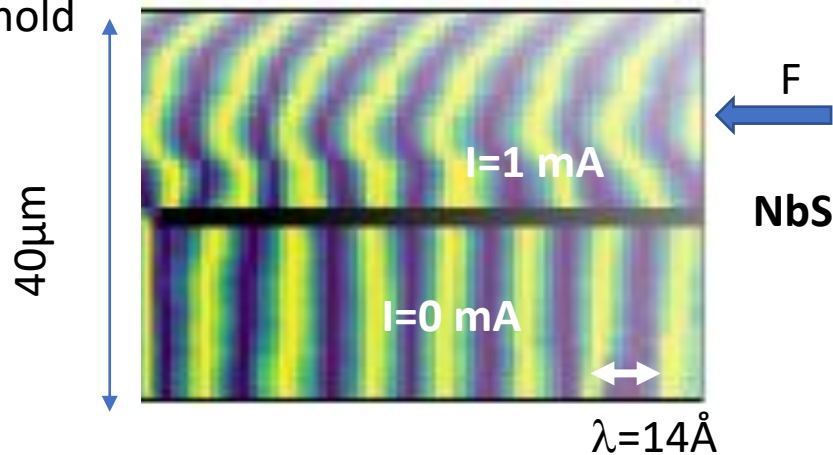
$\sim 5/7c$

4. External currents

a. small current: strong lateral surface pinning

Curvature of wave fronts (shear strain)

below threshold



E. Bellec et al., Phys. Rev. B 101, 125122 (2020)

Curvature at the nm scale, over tens of μm
Fast scanning diffraction (ID01 ESRF)



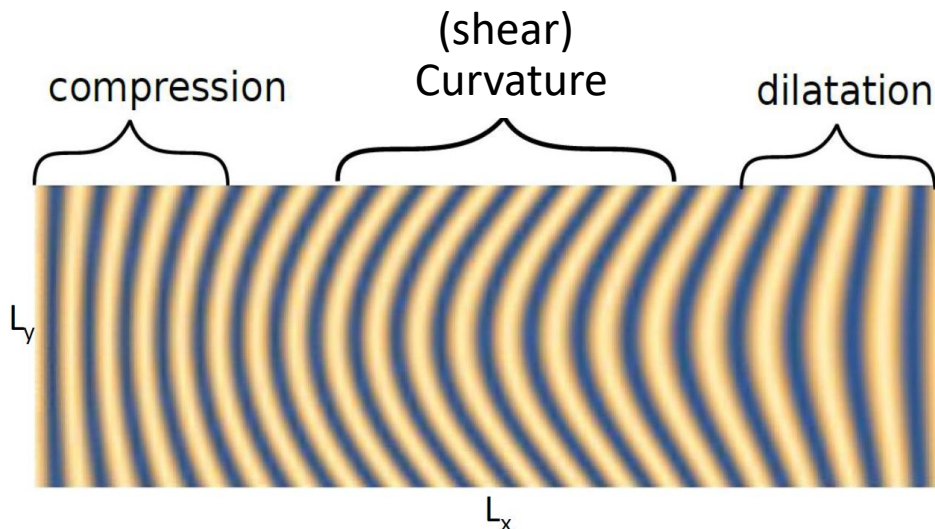
$$2 \left(c_x^2 \frac{\partial^2 \phi}{\partial x^2} + c_y^2 \frac{\partial^2 \phi}{\partial y^2} + c_z^2 \frac{\partial^2 \phi}{\partial z^2} \right) - \omega_0^2 \phi \approx \eta E$$

with the Dirichlet conditions:

$$\phi \left(\pm \frac{L'_x}{2}, y', z' \right) = \phi \left(x', \pm \frac{L'_y}{2}, z' \right) = \phi \left(x', y', \pm \frac{L'_z}{2} \right) = 0$$

2D guitar...

2 types of deformations: longitudinal/transverse



Green function + Charge image method

First order:

$$\phi(\vec{r}) \propto -E\eta\beta \cos\left(\pi \frac{x}{L_x}\right) \cos\left(\pi \frac{y}{L_y}\right) \cos\left(\pi \frac{z}{L_z}\right)$$

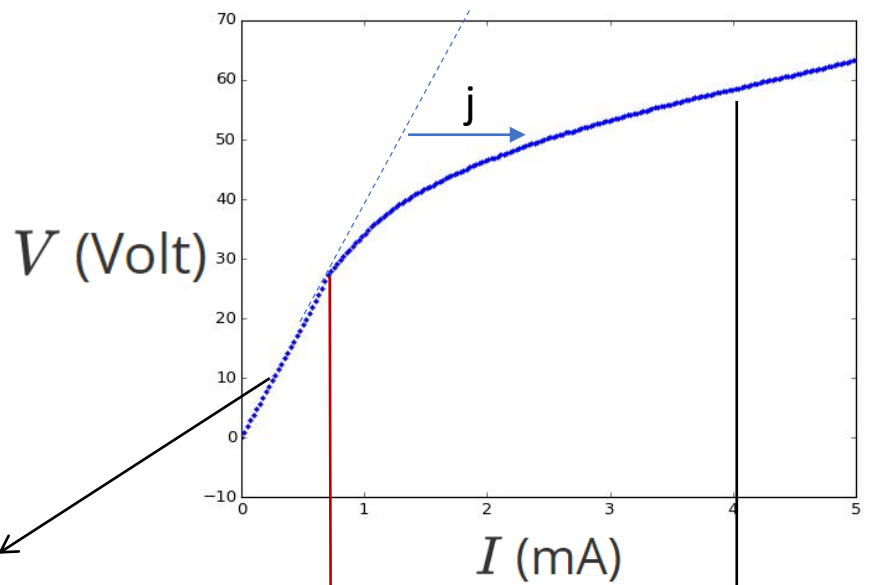
$$\beta = \frac{1}{\frac{c_x^2}{L_x^2} + \frac{c_y^2}{L_y^2} + \frac{c_z^2}{L_z^2} + \frac{\omega_0^2}{2\pi^2}}$$

E. Bellec et al., Eur. Phys. J. B (2020) 93: 165

4. External currents

b. Above the threshold: Incommensurate Charge Density Wave may slide

I-V characteristic



Ohm's law

Threshold current

I_s

An excess of current

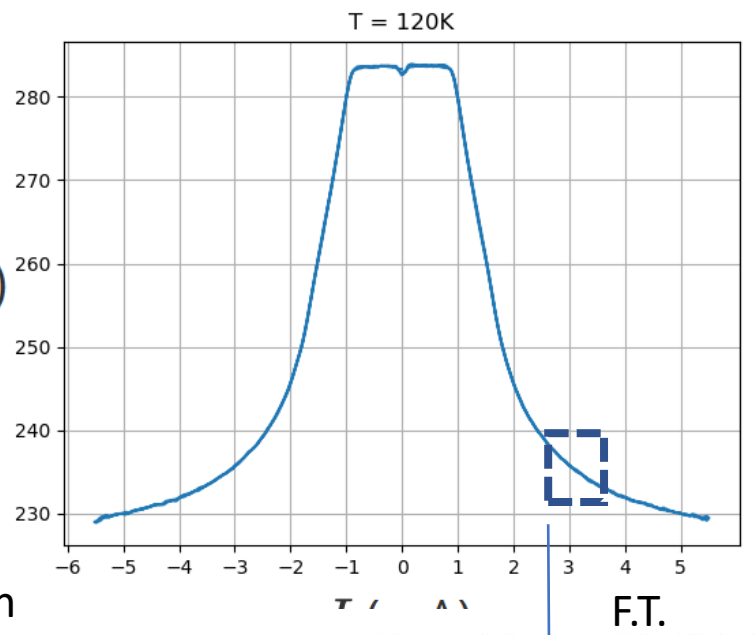
Nonlinearity I-V directly linked to the CDW

- Depining process (usual in condensed matter):
- Magnetic domain walls motion under B
- Dislocations nucleation under mechanical strain
- Vortices motion in superconductors with E

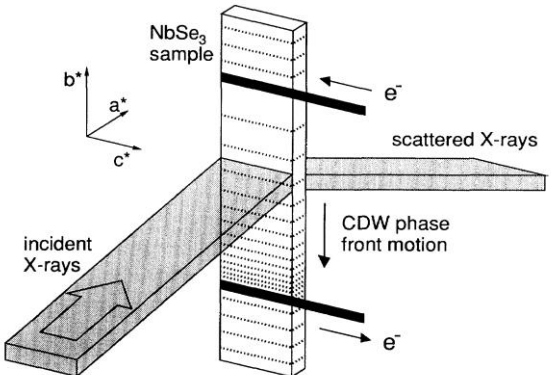
The charge transport in CDW :
it is a pulsed and collective mode which occurs on macroscopic scale

$$\frac{dV}{dI} \text{ (ohm)}$$

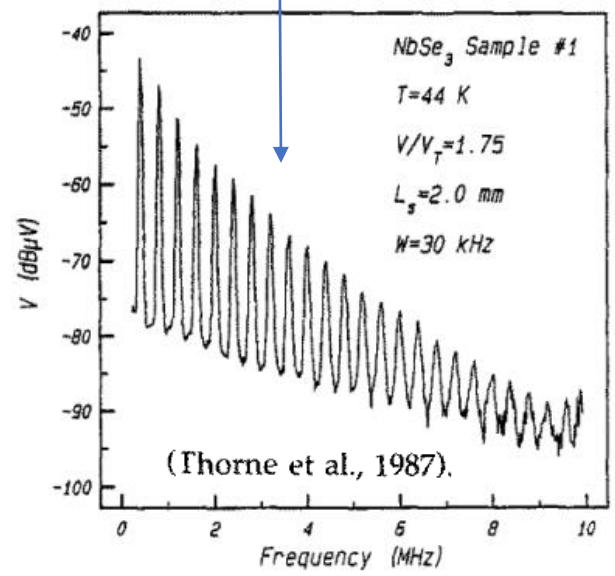
Differential resistivity as function of current in NbSe₃



Longitudinal deformation (compression/dilatation)



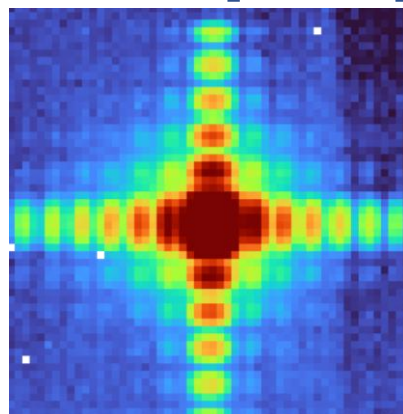
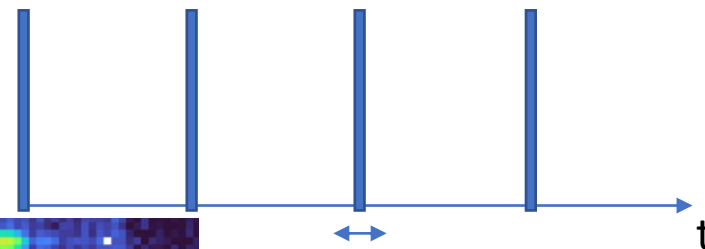
D. DiCarlo *et al.*, Phys. Rev. Lett. **70**, 845 (1993)
H. Requardt *et al.*, Phys. Rev. Lett. **80**, 5631 (1998)



XFEI source to obtain a global picture of sliding CDW



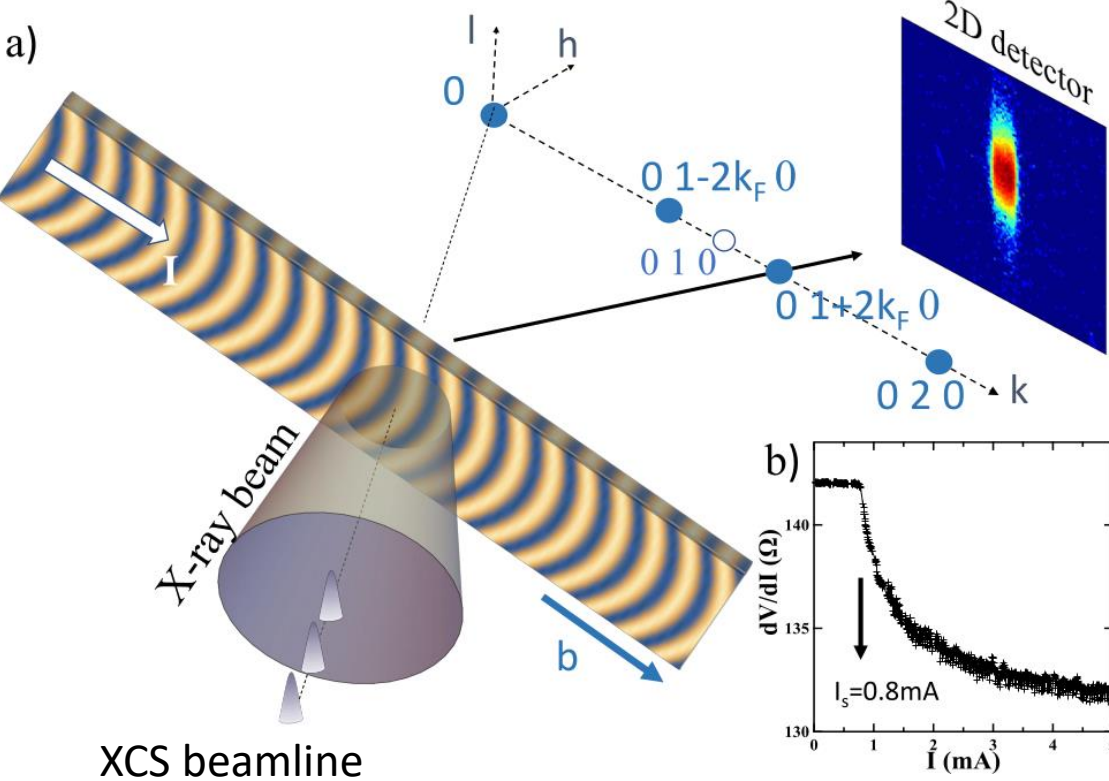
$\nu=120\text{Hz}$ ($t \sim 0,01\text{s}$)



Large and fully coherent beam

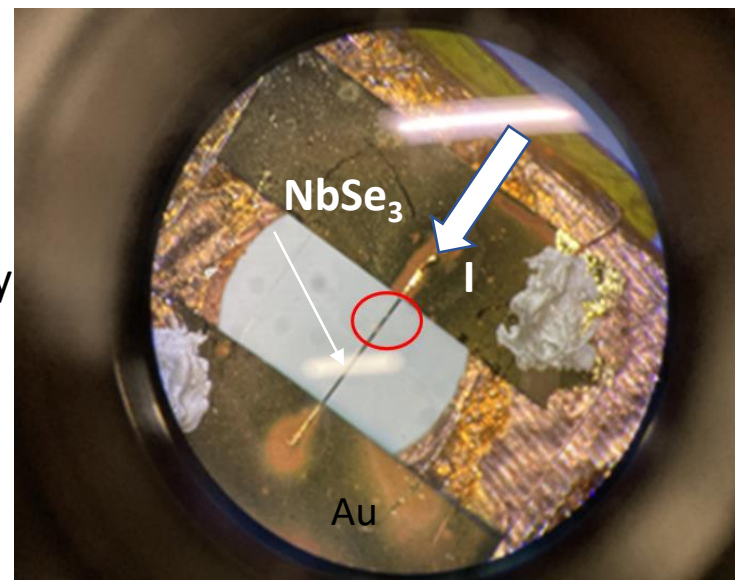
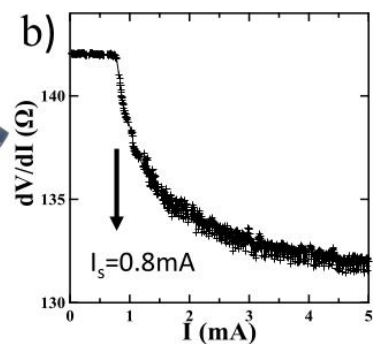
Slit diffraction $10\mu\text{m} \times 10\mu\text{m}$

Sample width $40\mu\text{m}$
 Sample thickness: $0.5\mu\text{m}$
 Sample-det= 8m
 Beam size $35\mu\text{m}$
 9.5keV



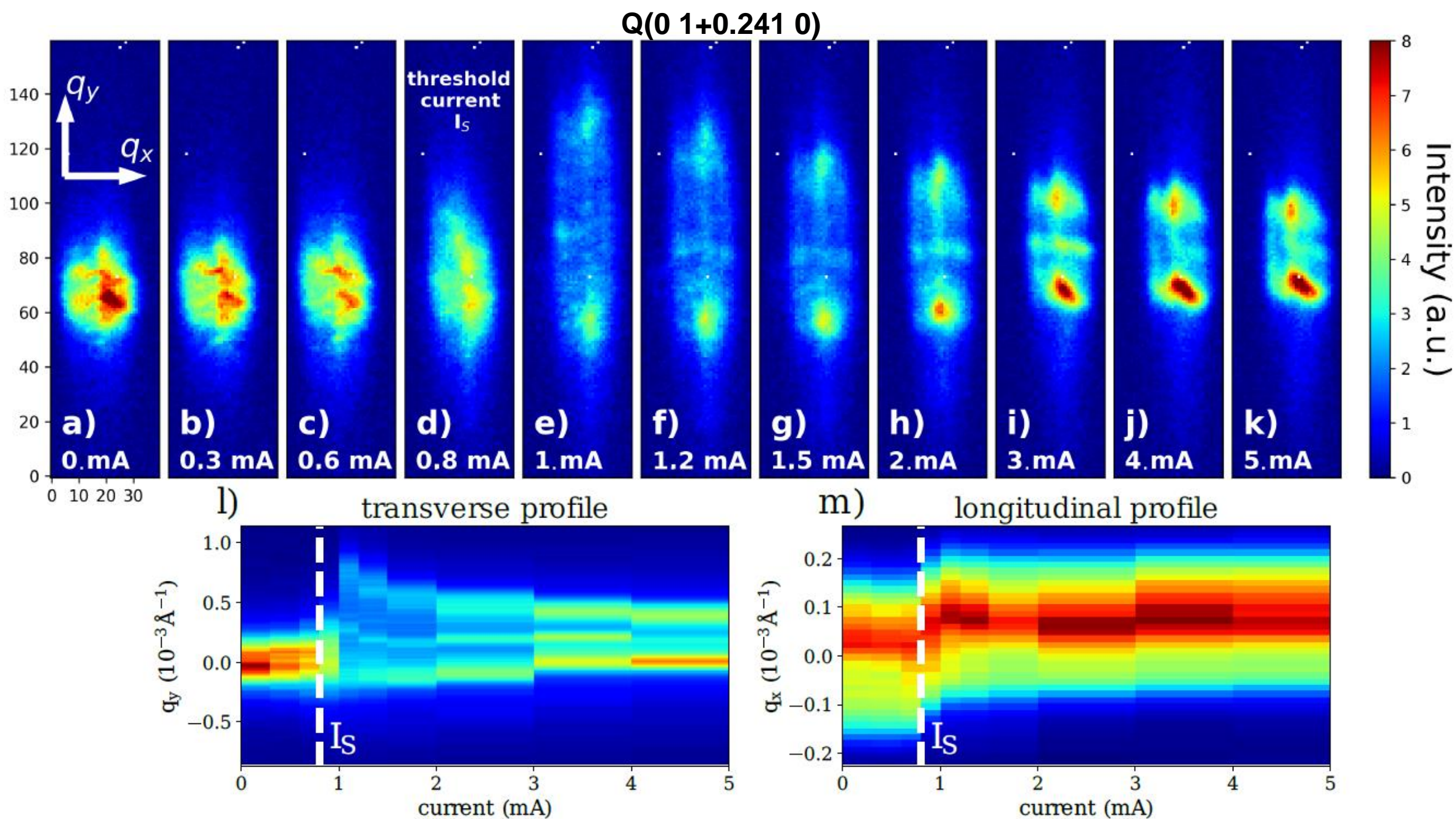
High brilliance

Stable satellite intensity from pulse to pulse

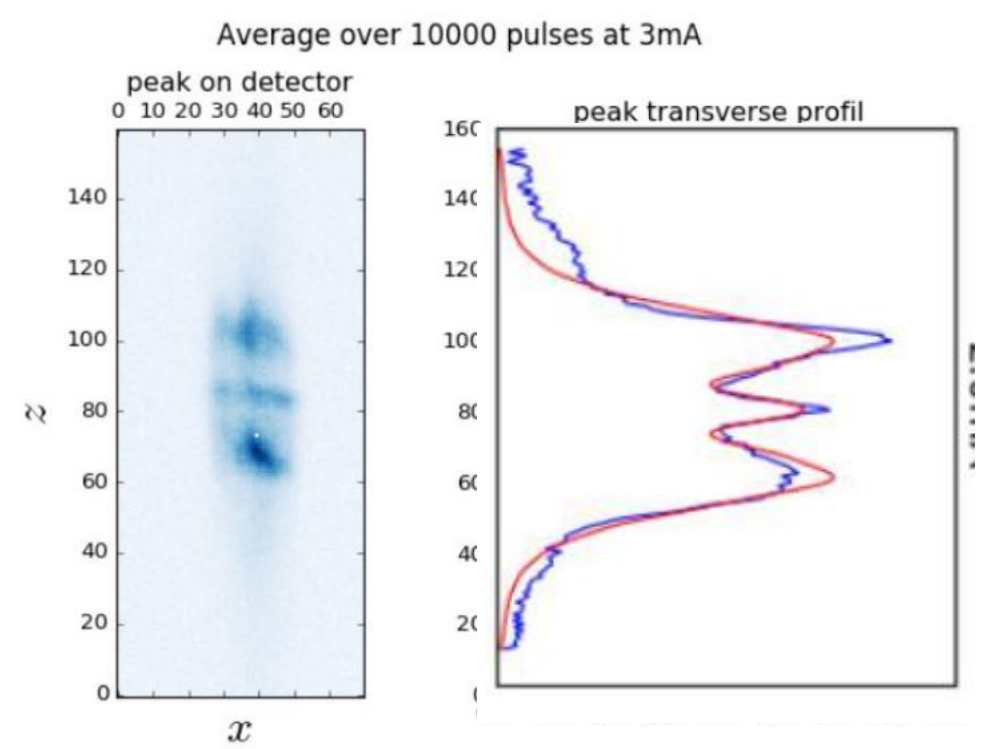
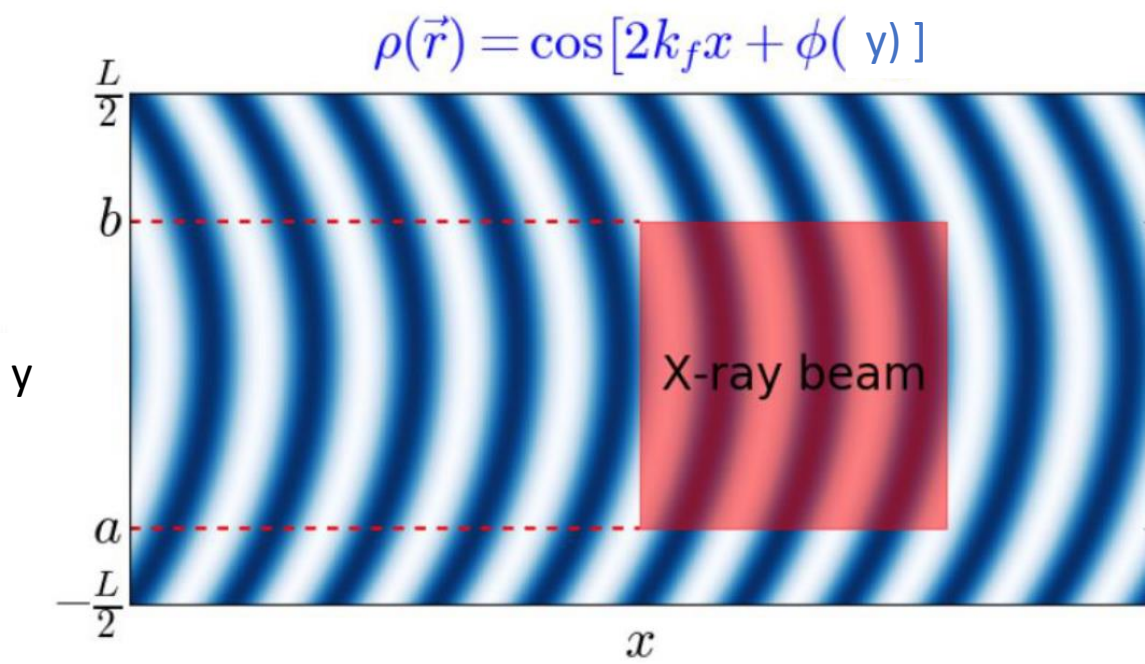


$T=80\text{k}$

($T_c=140\text{K}$)



Diffraction patterns versus current. (A) to (K) Integrated rocking curve of the $(0\ 1+q_s\ 0)$ satellite reflection associated to the CDW in NbSe₃ with increasing currents. The threshold current $I_S=0.8\text{mA}$ is indicated in (D).



Where $\rho(\vec{r})$ is the CDW charge density and $\phi(z) = -\frac{F}{2}(z - \frac{L}{2})(z + \frac{L}{2})$.

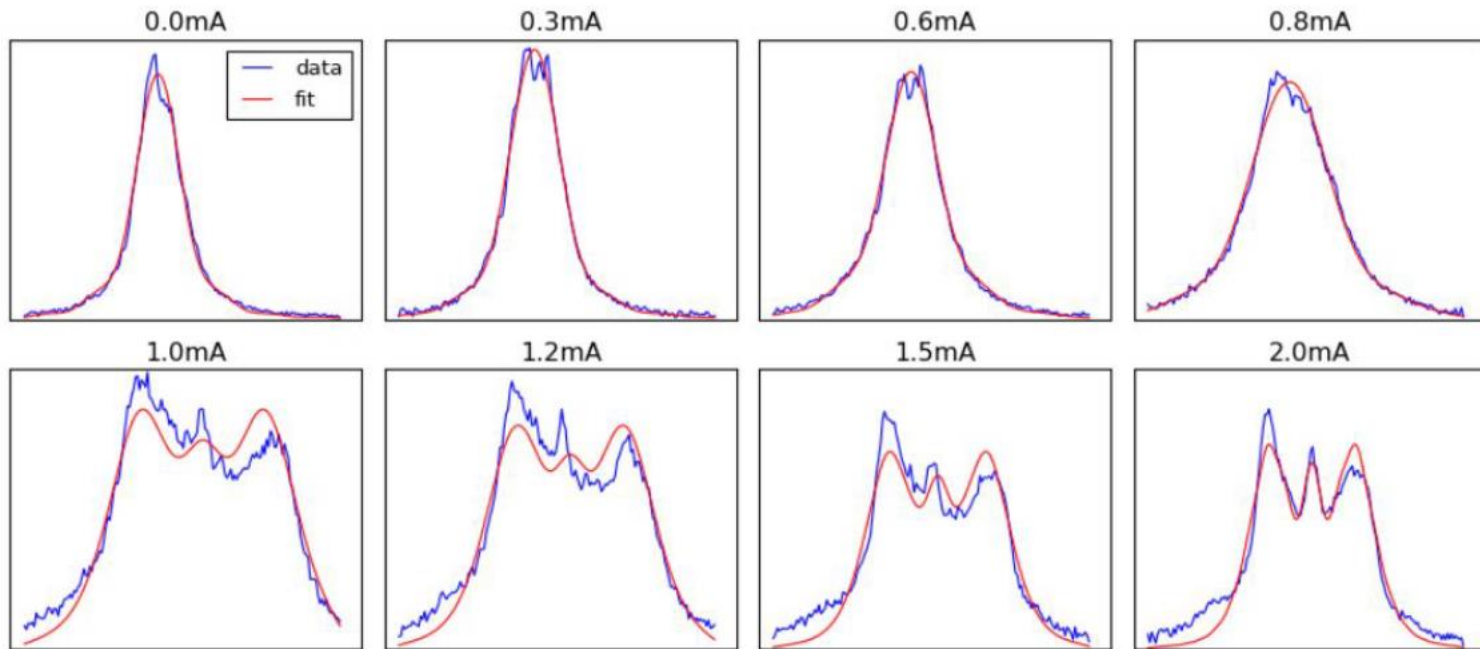
$$fit_{first\ try}(q_z) = |A_{fit}(q_z)|^2 = \frac{\pi C}{2F} \left| \operatorname{erfi} \left[\frac{(1+i)(aF - q_z)}{2\sqrt{F}} \right] - \operatorname{erfi} \left[\frac{(1+i)(bF - q_z)}{2\sqrt{F}} \right] \right|^2$$

where erfi is the imaginary error function $\operatorname{erfi}(z) = \frac{\operatorname{erf}(iz)}{i}$.

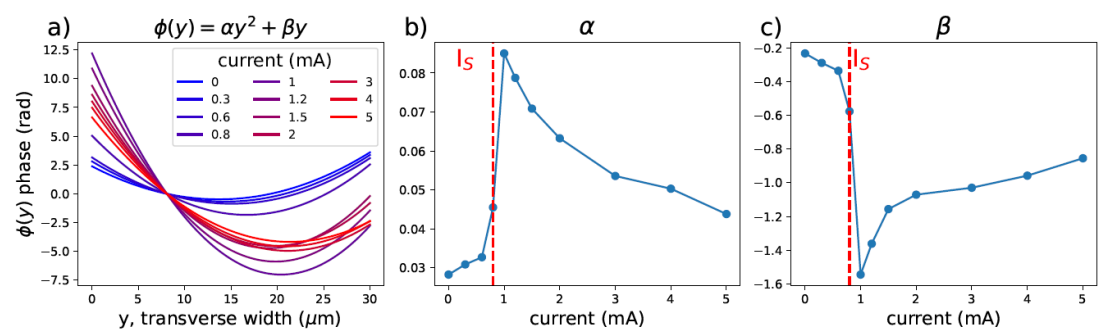
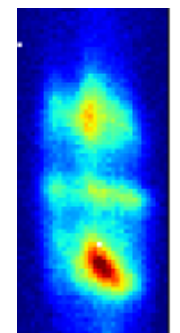
$$fit_{second\ try}(q_z) = fit_{first\ try}(\alpha q_z)$$

$$fit_{p_1, p_2, p_3, p_4, p_5}(q_z) = fit_{second\ try; p_1, p_2, p_3, p_4}(q_z) \otimes Gauss(q_z, p_5)$$

Fit considering a quadratic phase $\phi(y) = \alpha y^2 + \beta y$



Impossible to fit the assymetry...



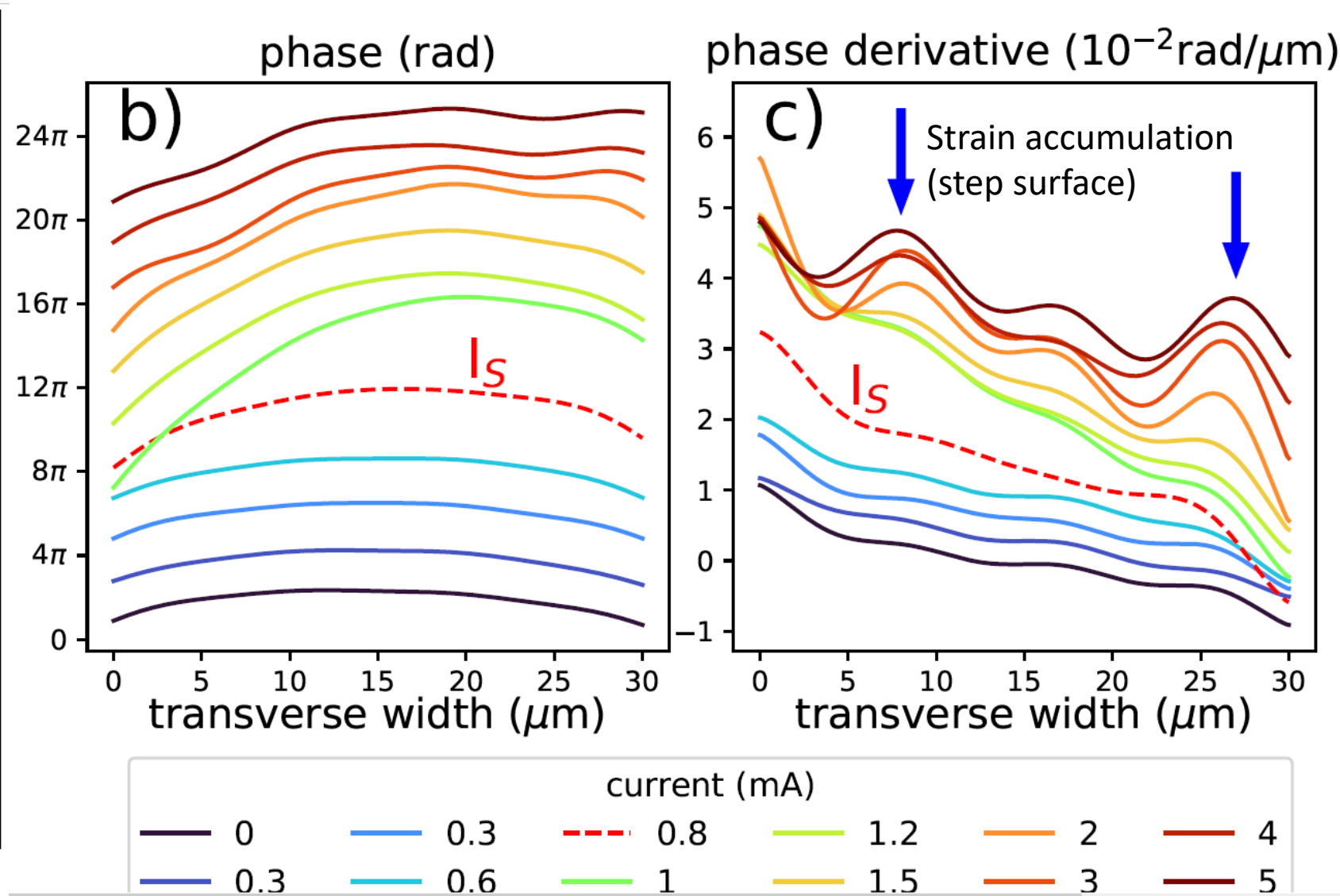
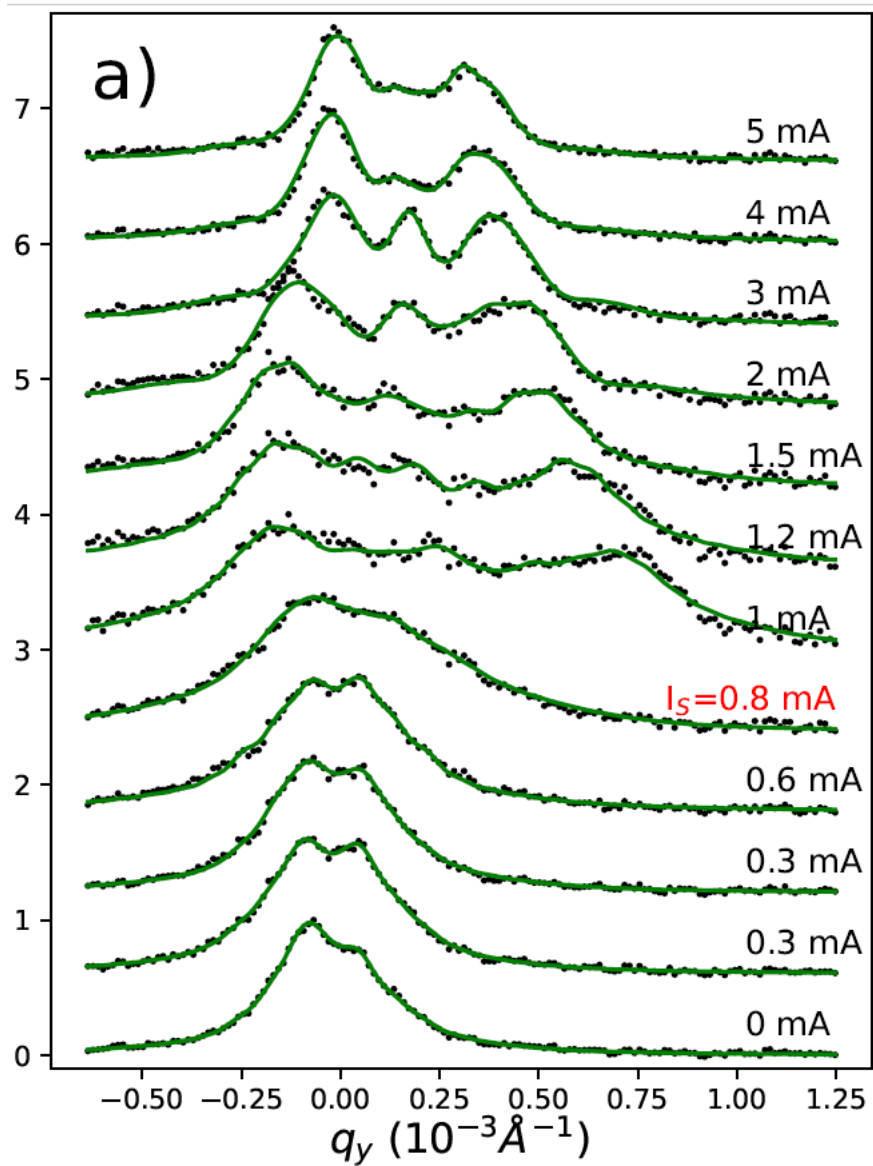
Phase retrieval: Genetic algorithm called Differential-Evolution (DE).
 Stochastic process and iterative method: efficient for discontinuous or noisy case (not a gradient method)

$$\phi(y) = c_1 \cos\left(\pi \frac{y}{L_y}\right) + \sum_{n=2}^6 [c_n \cos\left(n\pi \frac{y}{L_y}\right) + s_n \sin\left(n\pi \frac{y}{L_y}\right)] + \alpha y$$

R. Storn and K. Price, Journal of global optimization 11, 341 (1997).
 M. K. M.Wormington Matthew, Panaccione Charles and B. D. Keith Phil. Trans. R.Soc. **A.357**, 2827 (1999) (1999).
 S. Das and P. N. Suganthan, 15, 4 (2010).

Elastic model:

$$\phi(\vec{r}) \propto -E\eta\beta \cos\left(\pi \frac{x}{L_x}\right) \cos\left(\pi \frac{y}{L_y}\right) \cos\left(\pi \frac{z}{L_z}\right)$$



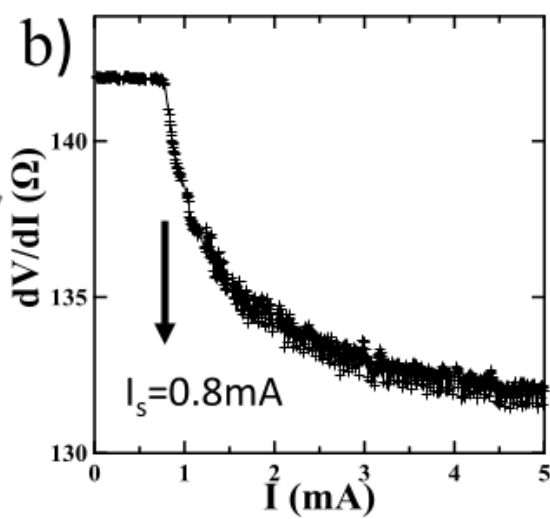
Shear component:

$$e_{xy} = e_{yx} = -\frac{1}{2} \frac{1}{q_s} \frac{\partial \phi}{\partial y}$$

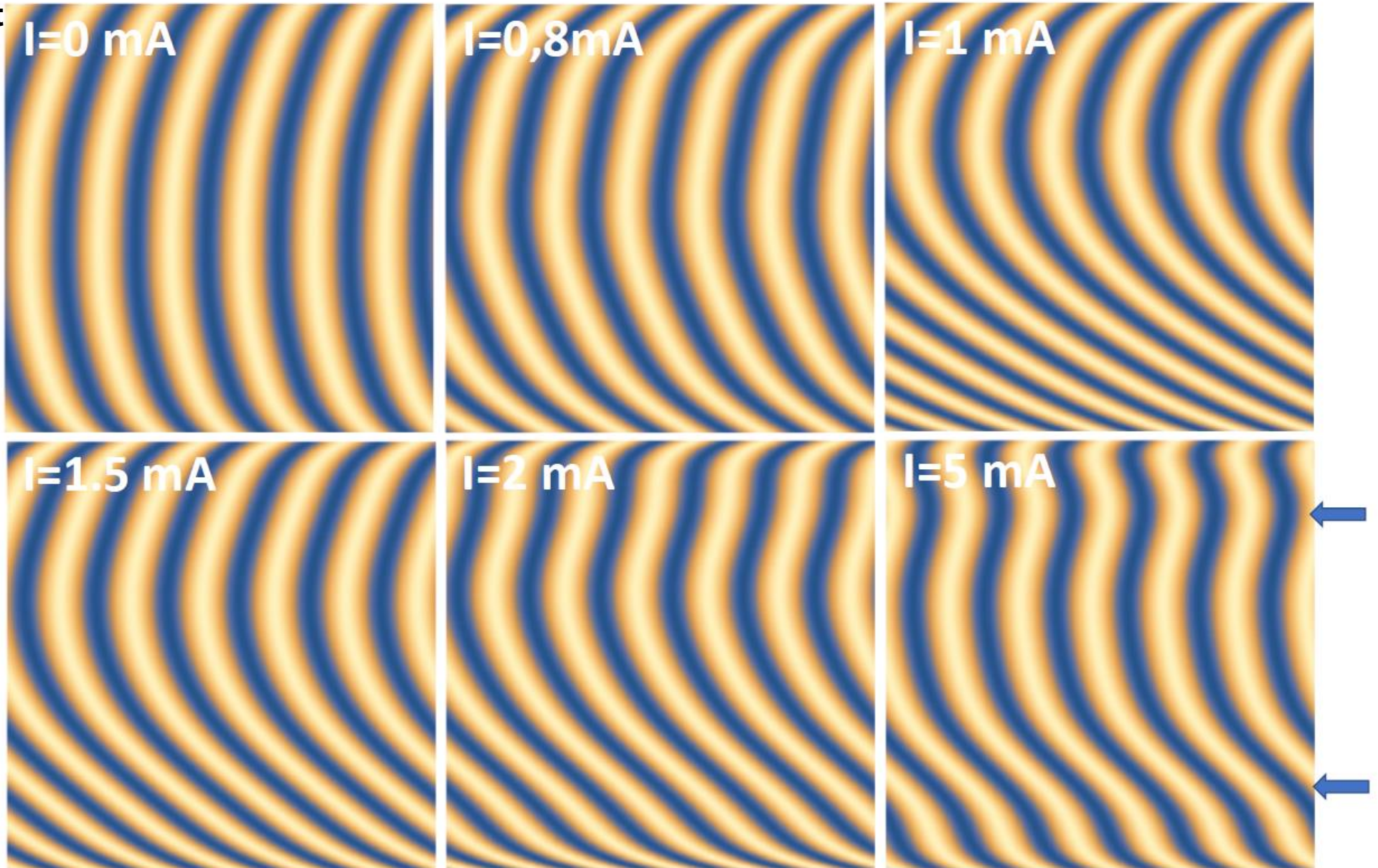
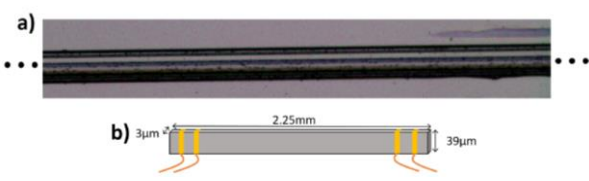
$$\Phi(y) \sim (y - l_y/2)(y + l_y/2)$$

$$\Phi'(y) \sim 2y$$

CDW state versus current

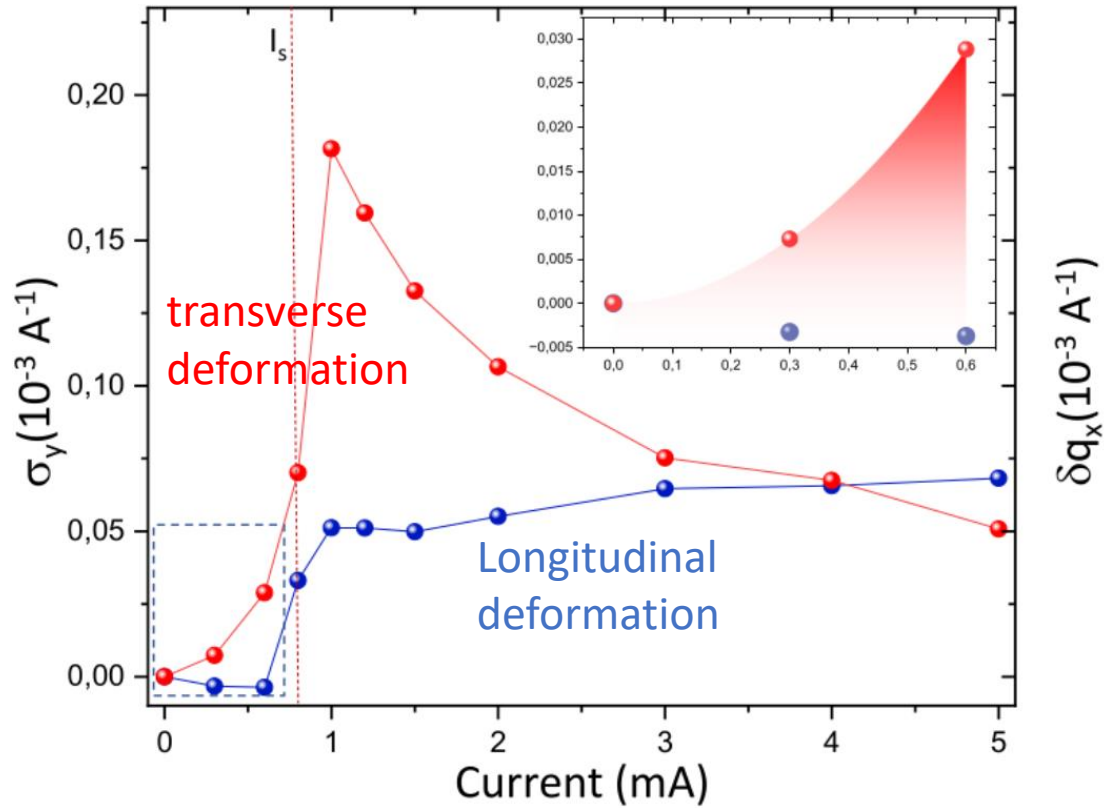


Sample image

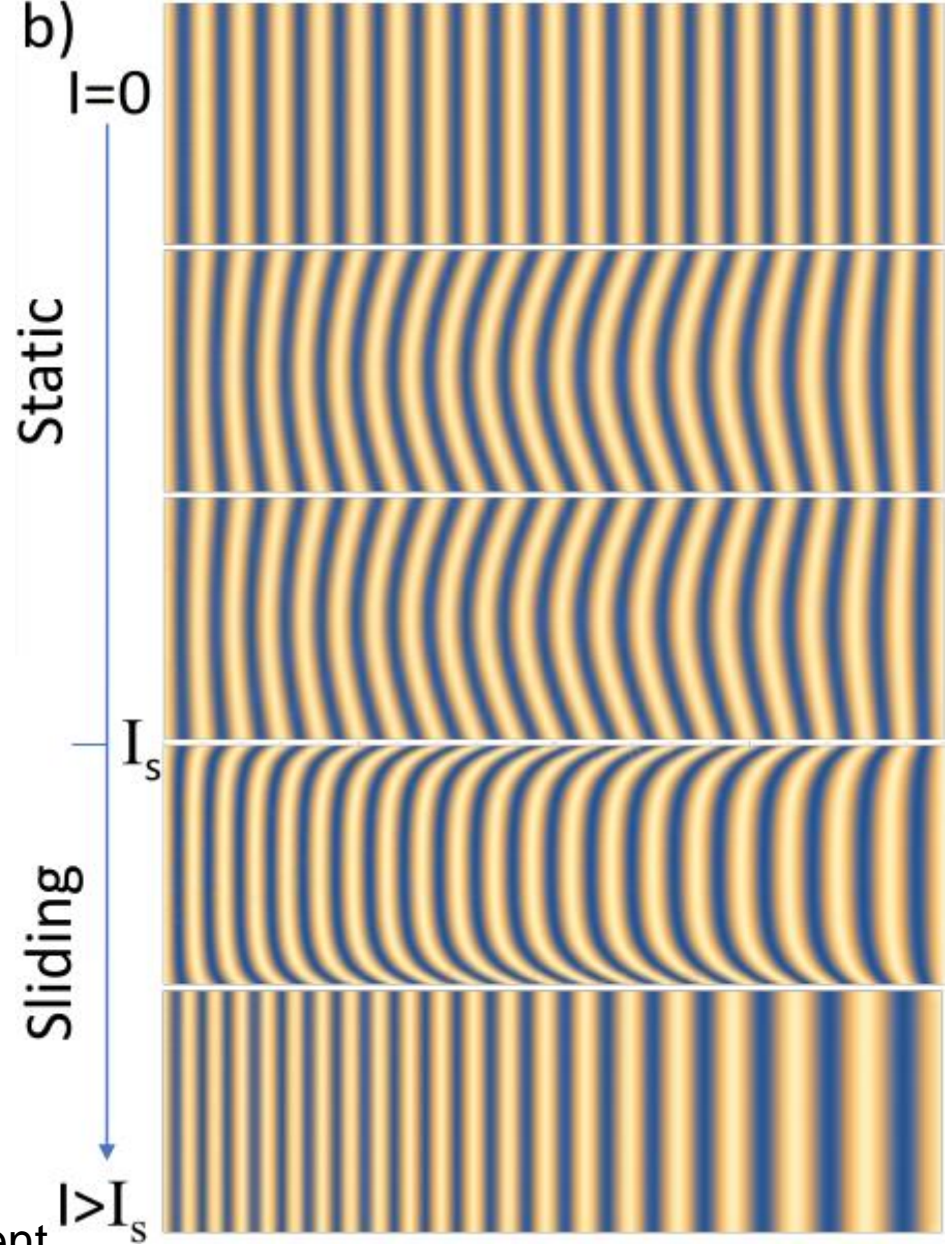


2D maps of the CDW state corresponding to 6 currents, below and above the threshold field ($I_s=0.8 \text{ mA}$) by using the CDW phase obtained from the fit. Wavefronts corresponding to a constant phase are represented in yellow. The two arrows show surface step position.

Transverse versus longitudinal deformations: closely linked



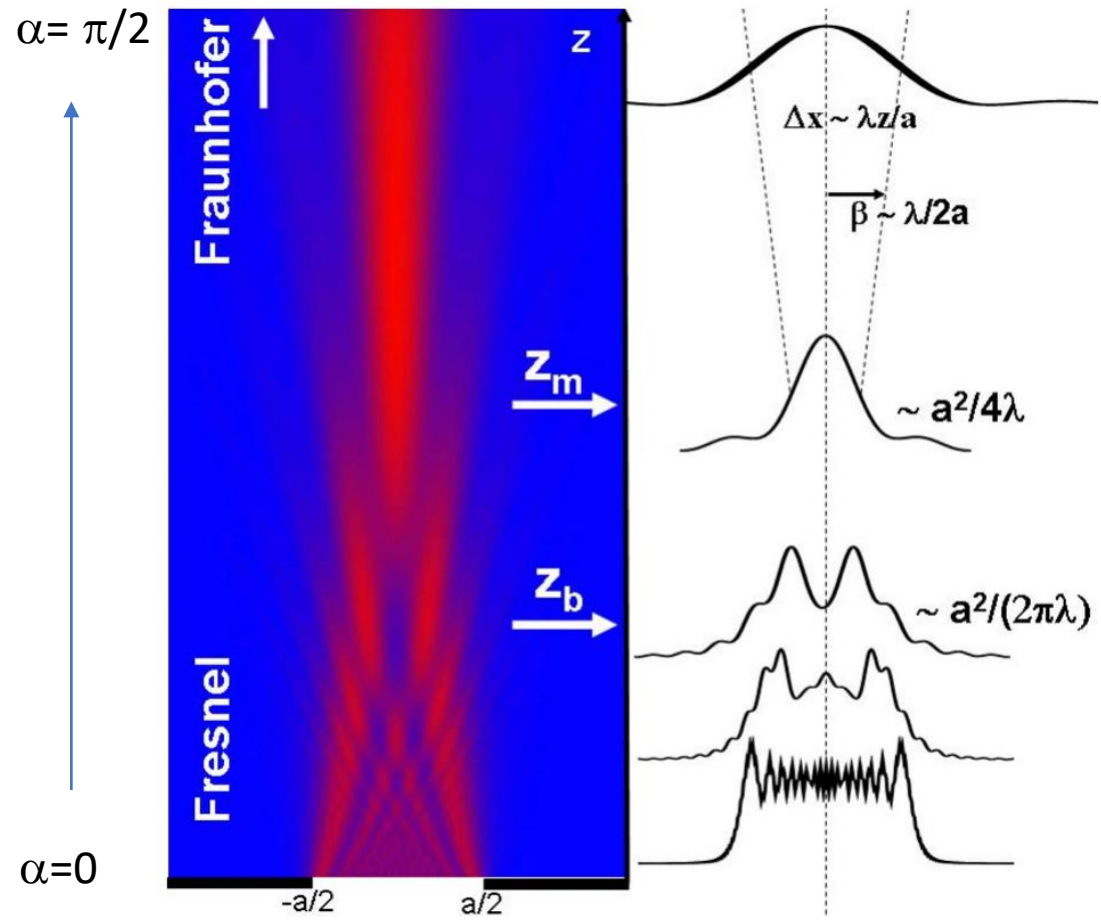
$$2 \left(c_x^2 \frac{\partial^2 \phi}{\partial x^2} + c_y^2 \frac{\partial^2 \phi}{\partial y^2} + c_z^2 \frac{\partial^2 \phi}{\partial z^2} \right) - \omega_0^2 \phi \approx \eta E$$



CDW deformation obtained by decreasing the ratio $c_y < c_x$ with current.

Although this static model is phenomenological, it does reproduce the overall situation observed here, with an increasing compression and a decrease in curvature between two pinning centers above threshold.

Below threshold: Optical interpretation



Hard x-Rays
Dark point
position=1m
a=10μm
λ=1Å

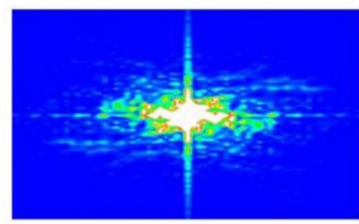
$$\mathcal{F}_\alpha[g](q) = \int_{-\infty}^{\infty} K(q, x)g(x)du$$

$$K(q, x) = \sqrt{\frac{1 - i \cot \alpha}{2\pi}} \exp\left[-i \frac{qx}{\sin \alpha} + \frac{i}{2}(q^2 + x^2) \cot \alpha\right]$$

Manet (1872)
Berthe Morisot



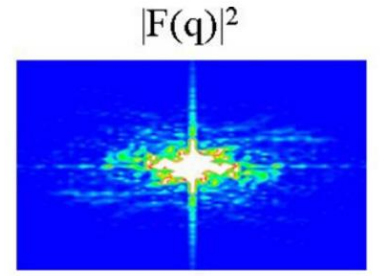
$$(\mathcal{F}^4 f)(x) = (\mathcal{F}(\mathcal{F}f))(-x) = f(x)$$



|F(q)|²

The Fractional Fourier transform

$$F(q) = \mathfrak{F}f(x)$$

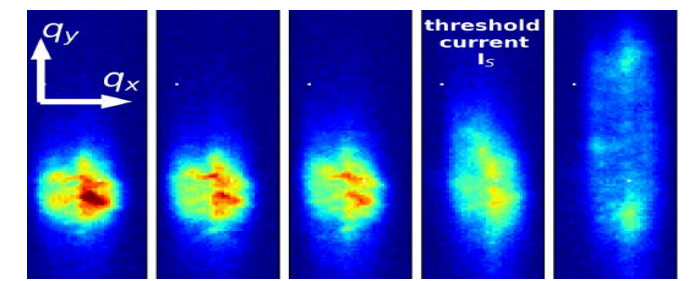


|F(q)|²

$$(\mathcal{F}^2 f)(x) = (\mathcal{F}(\mathcal{F}f))(x) = f(-x)$$



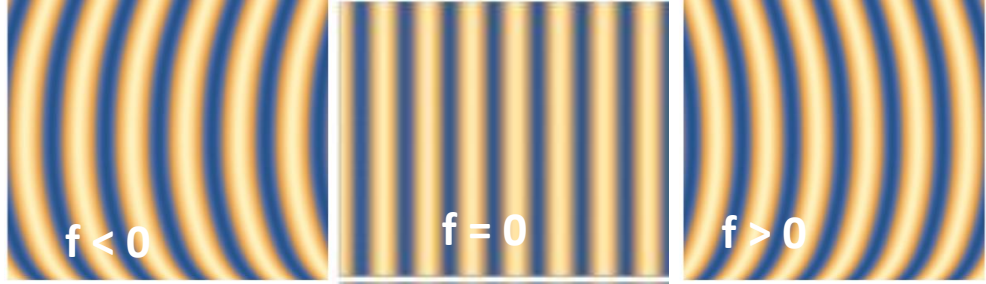
FracFT: rotation de π/2
α=0 identity
α= π/2 Fourier Transform



V. Namias, J. Inst. Math. Appl. **25**, 241 (1980)
Le Bolloc'h, D and Sadoc, Eur. Phys. J. B, 81 (4): 481–487 (2009)

Diffraction of a bent CDW

$$\mathcal{F}_\alpha^f(q) \propto \int_{-a}^a \exp\left[-i\frac{qx}{\sin \alpha} + \frac{i}{2}(q^2 + x^2) \cot \alpha\right] \exp[i2k_F x] \exp[if(x^2 - a^2)] dx$$



$$\mathcal{F}_\alpha^f(q) = \mathcal{F}_{\alpha'}^0(q')$$

$$\cot \alpha' = \cot \alpha + 2f$$

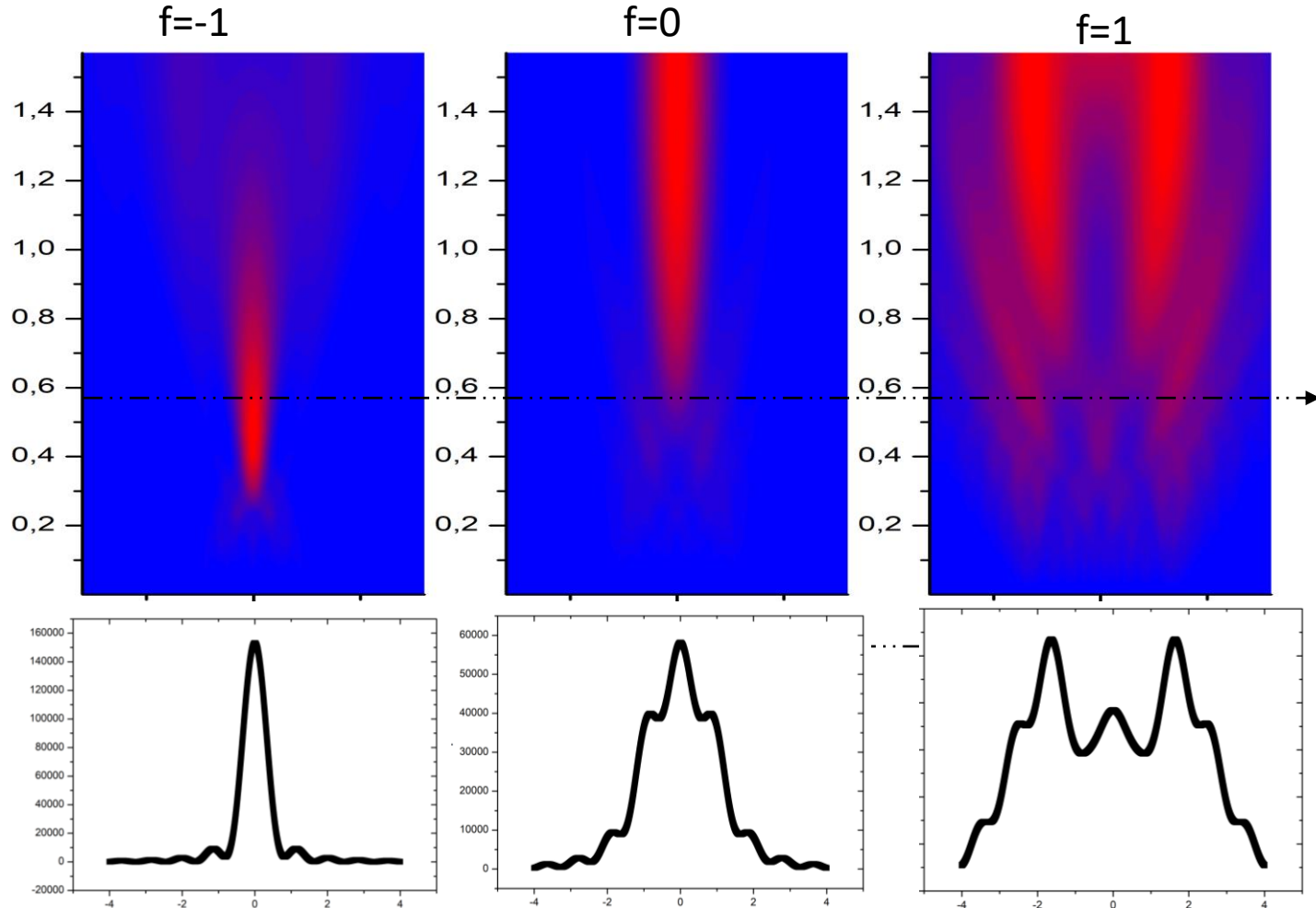
$$q'/q = \frac{1}{\sqrt{1 + (\cot \alpha + 2f)^2}}$$

Space curvature \longrightarrow Contraction/dilatation of space and time

A tunable electronic lens for hard X-rays ?

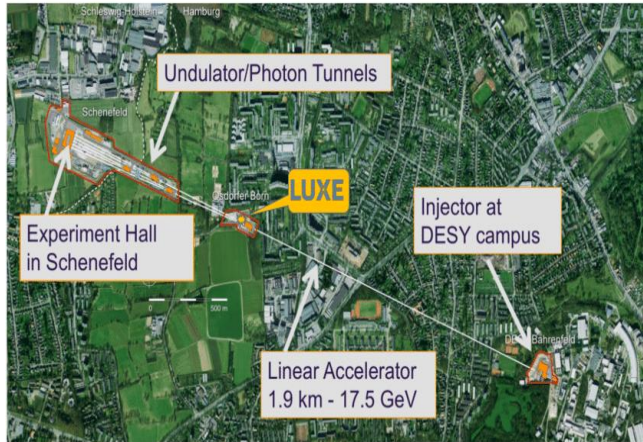
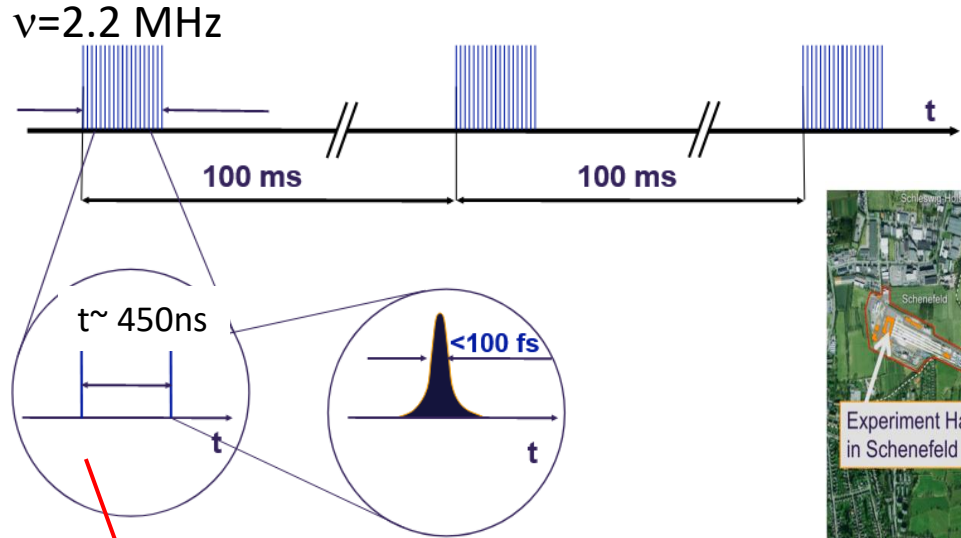
Not reflective lens (Kirkpatrick–Baez systems, capillaries, waveguides)
 Not refractive (Be lenses)
 and diffractive (Fresnel zone plate) optics.

Continuous tunable lens, driven by a small applied electric field (either positive/negative; convergent/divergent lens playing with Fresnel/Fraunhofer regime)
 With restrictions
 In 1D only/ Intensity ?



E-XFEL / MID beamline

Charge density wave submitted to an external dc current

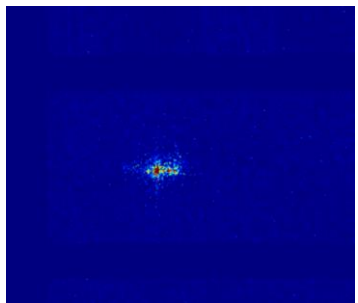


• Beam properties :

- i. $E = 9 \text{ keV}$
- ii. Seeding mode
- iii. Pink beam
- iv. pulse energy $\sim 0.5 \text{ mJ} = 3 \cdot 10^{11}$ photons/pulse at 10 keV.

• Time Structure :

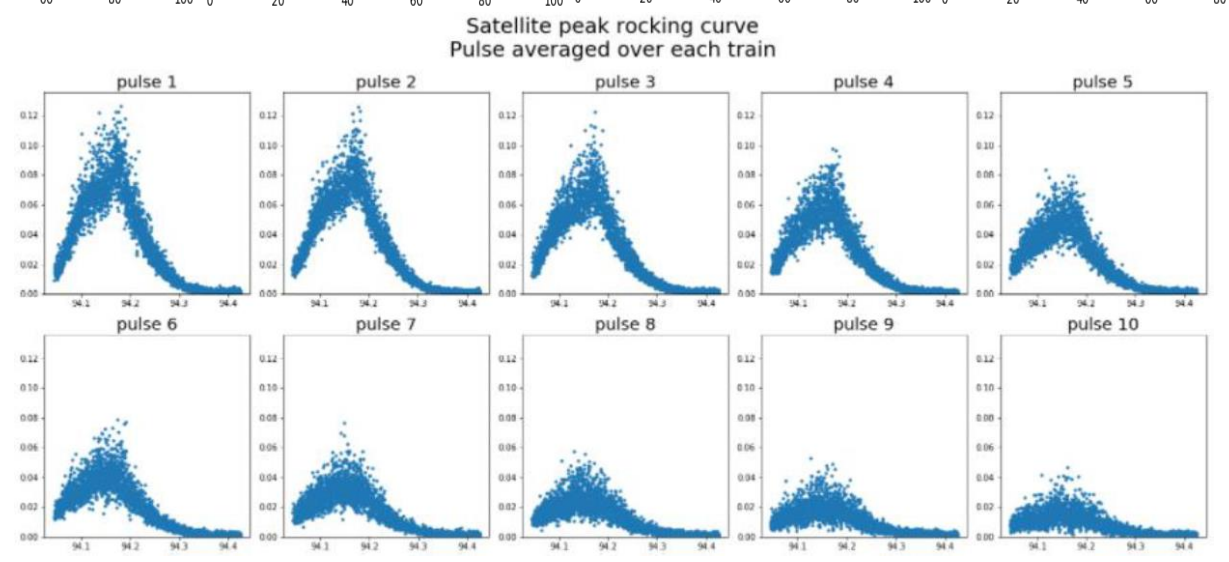
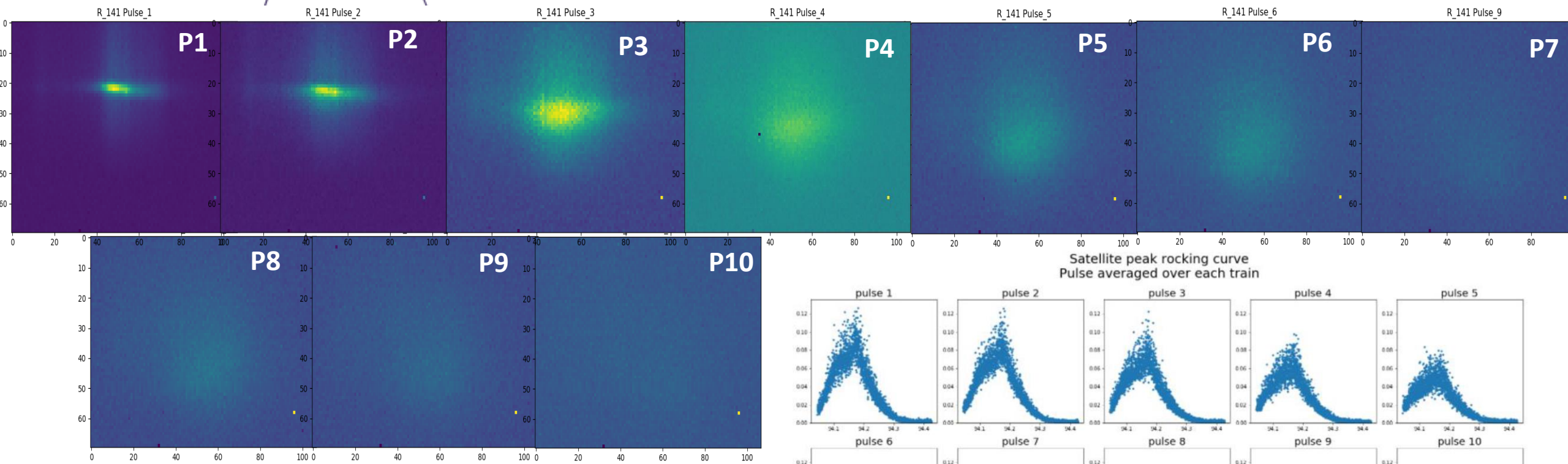
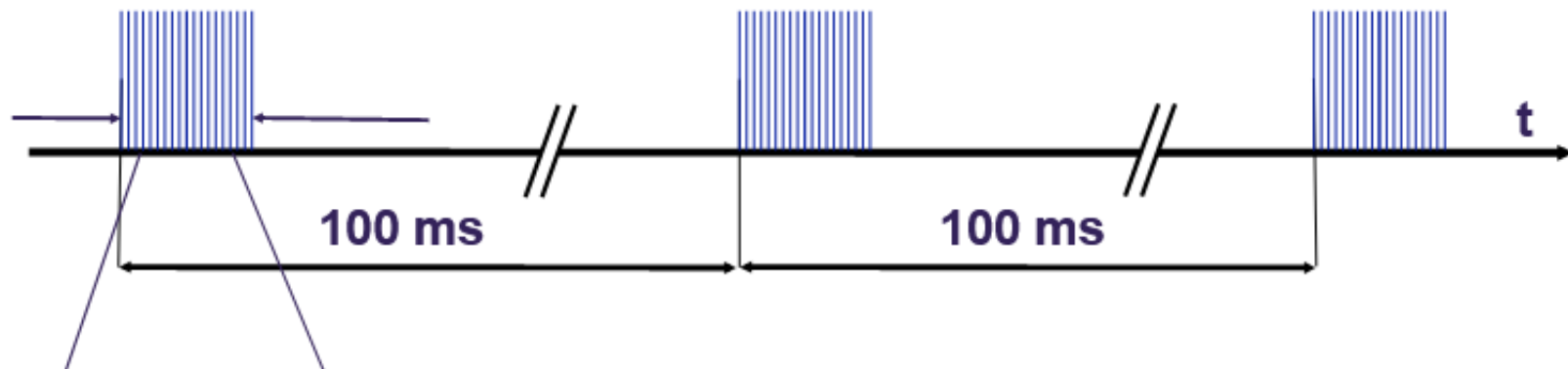
- i. pulse duration $< 100 \text{ fs}$
- ii. 10 pulse trains/s (1 train each 100 ms = 0.1 s)
- iii. Each train is made of pulses (1~60 pulses/train)
- iv. Intra-bunch up to 2.2 MHz:
i.e. $\Delta t = 450 \text{ ns}$ spacing between single pulses



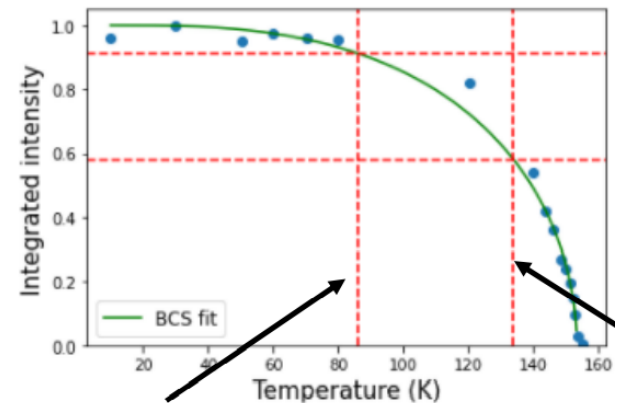
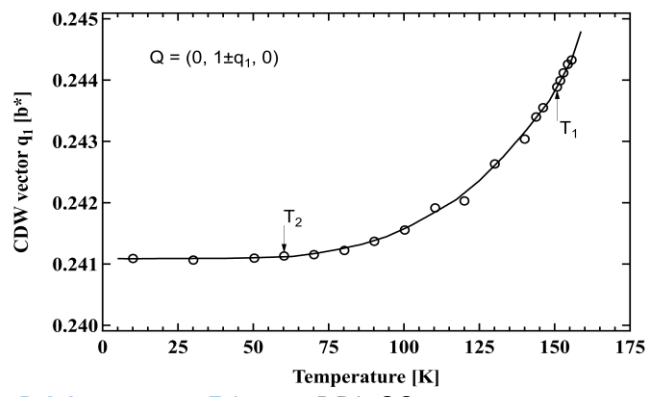
Stable from train to train, but ...

$Q(0 \ 1.241 \ 0) \text{ NbSe}_3$

High resolution obtained from a single pulse

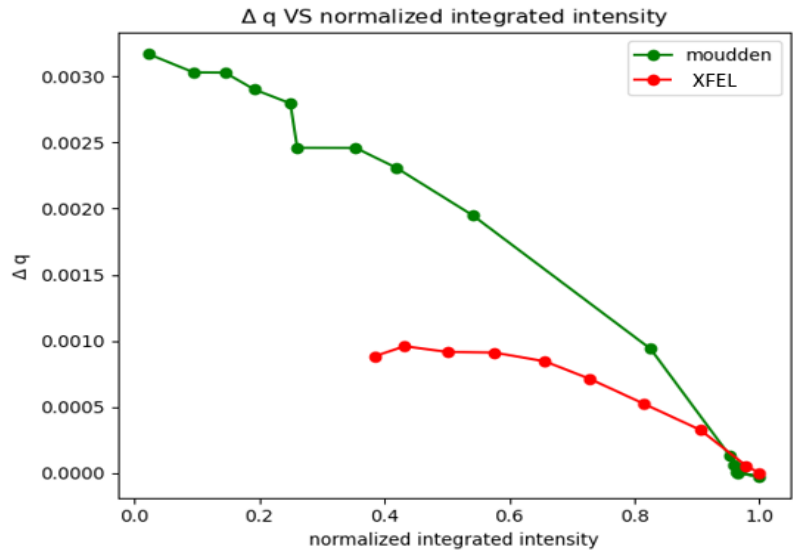


Heating effect ?

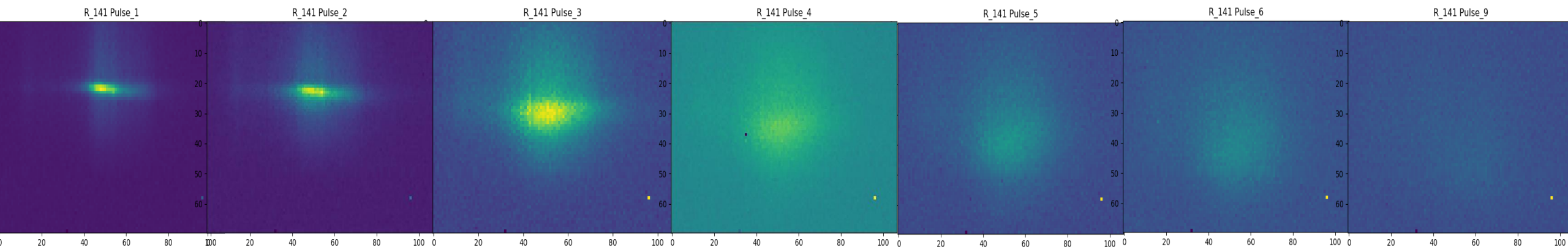


[AH Moudden](#), [JD Axe](#), [P Monceau](#), [F Levy](#), PRL 90

X-rays from XFEL sources pump and probe CDW systems
Out-of equilibrium



Same nature of the pump and probe
Split and delay ?



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Thank you for your attention

